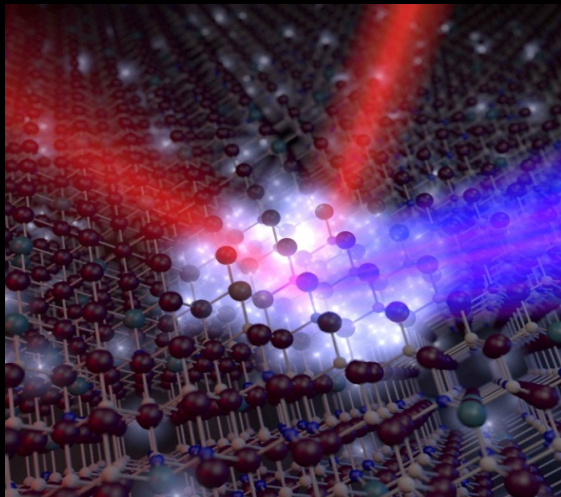


# METAMATERIALS: TECHNOLOGY OF THE FUTURE



“To move, to breathe, to fly, to float,  
To gain all while you give,  
To roam the roads of lands remote,  
**To travel is to live.”**

— Hans Christian Andersen, *The Fairy Tale of My Life: An Autobiography*

# OUTLINE

## Brief intro to metamaterials

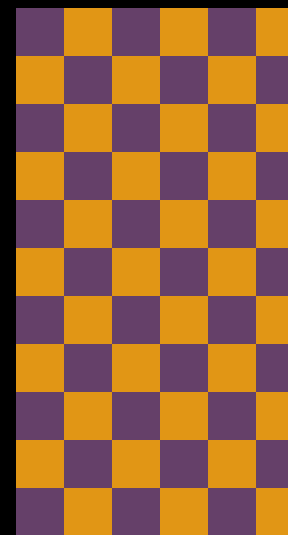
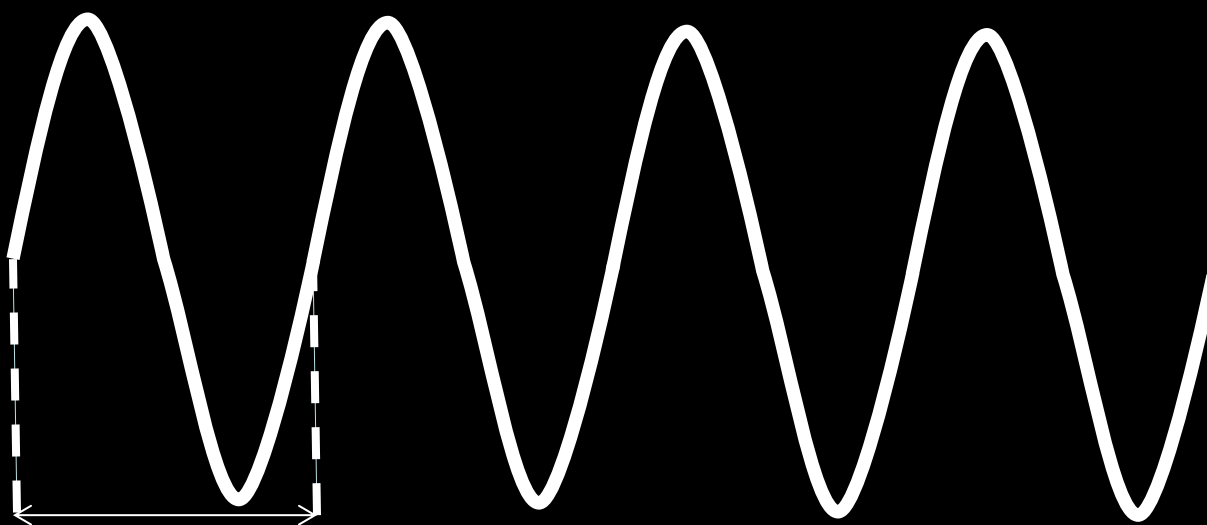
- Electrical metamaterials (plasmonics) for nanophotonics
- Magnetic metamaterials and negative refractive index
- Seeing a DNA in Optical Microscope?
- Cloaking: SciFi or reality?
- 2D metamaterials: Metasurfaces



# METAMATERIALS

Is it possible to engineer materials with **NEW OPTICAL PROPERTIES?**

- **YES!**
- Wonderful things happen when structural dimensions are much less than  $\lambda$  light!
- Road to **NEW OPTICS** and **NEW TECHNOLOGIES**



Wavelength  
~ 500nm

~ 50nm

## ELECTROMAGNETIC PROPERTIES

## V.S. SIZES

0

1

 $\infty$ 

SIZE/WAVELENGTH

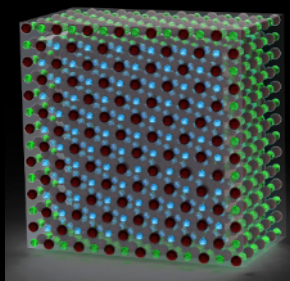
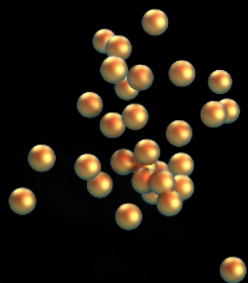
size  $\ll \lambda$ 

Crystals



PLASMONICS

METAMATERIALS

size  $\sim \lambda$ 

Diffraction

Interference

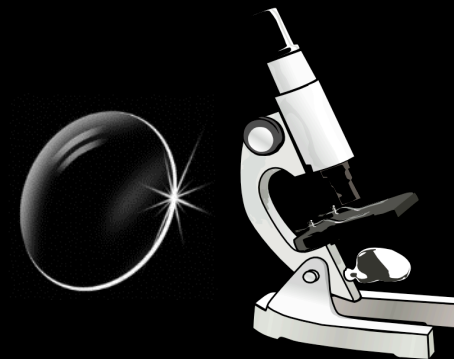
Gratings

size  $\gg \lambda$ 

Geometrical Optics

Lenses

Shadows



Scientists have gone from BIG LENSES, to OPTICAL FIBERS, to  
ULTRA-SMALL/THIN DEVICES with unique functionalities using METAMATERIALS

# WHY WE NEED METAMATERIALS?

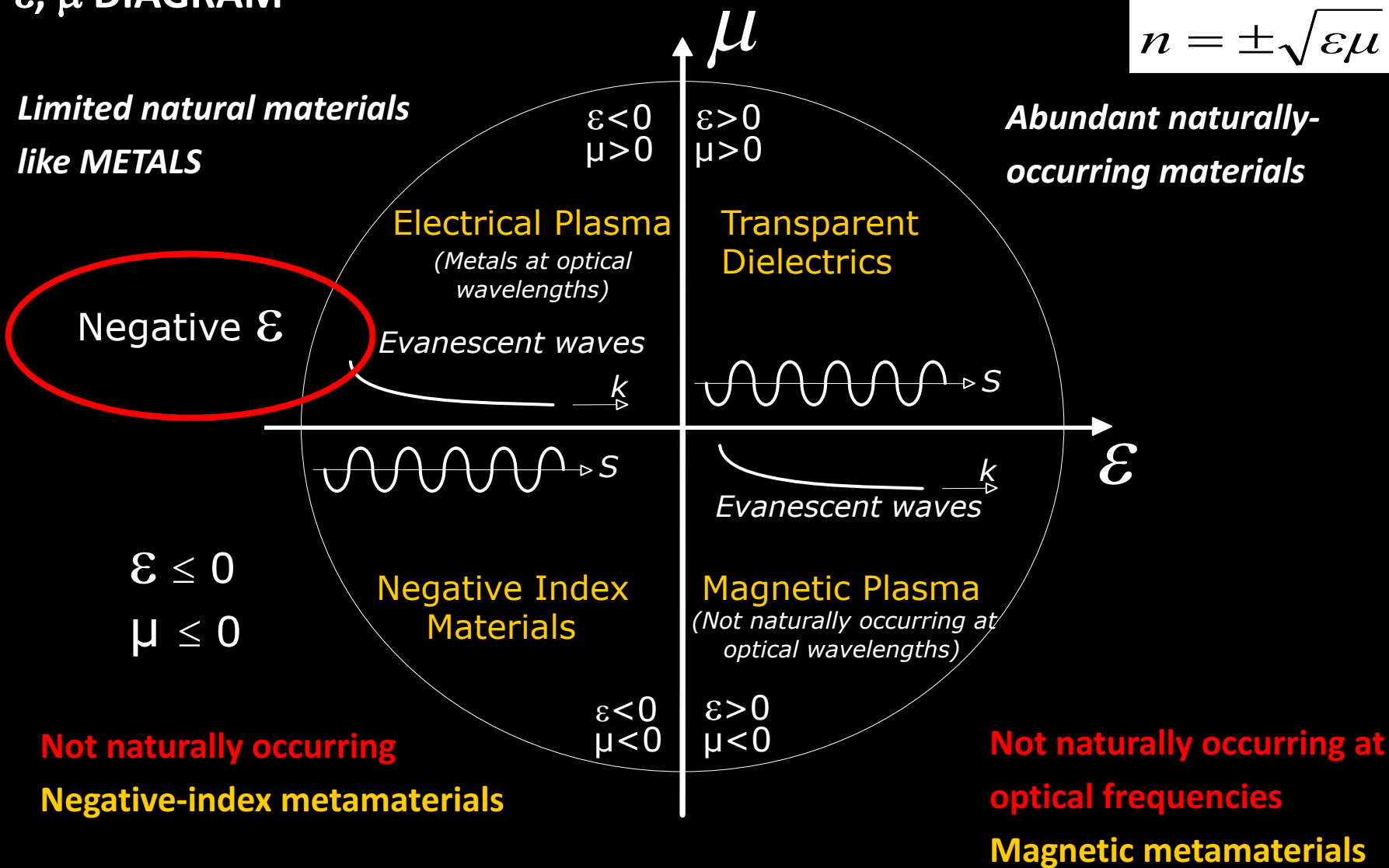
$$n^2 = \epsilon\mu$$

$$n = \pm\sqrt{\epsilon\mu}$$

## $\epsilon, \mu$ DIAGRAM

Limited natural materials like METALS

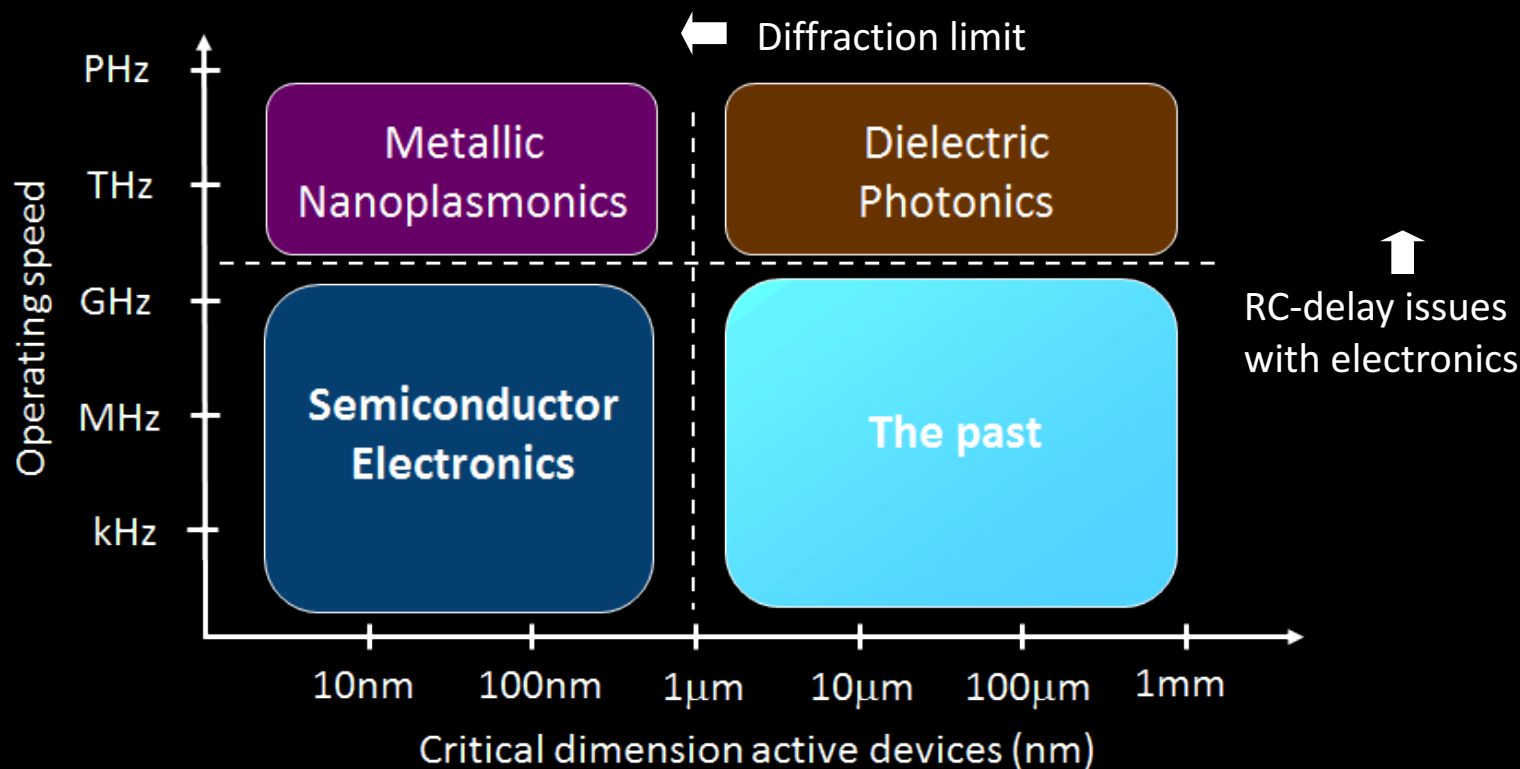
Abundant naturally-occurring materials



# Electrical Metamaterials (Plasmonics): a Route to Nanophotonics

# WHY ELECTRICAL METAMATERIALS?

## Operating regimes of different technologies



- Improved synergy between electronic and photonic devices
- Solution to the size-compatibility problem
  - Plasmonics naturally interfaces with *similar size electronic components*
  - Plasmonics naturally interfaces with *similar operating speed photonic networks*

# ELECTRONIC-PHOTONIC INTEGRATION

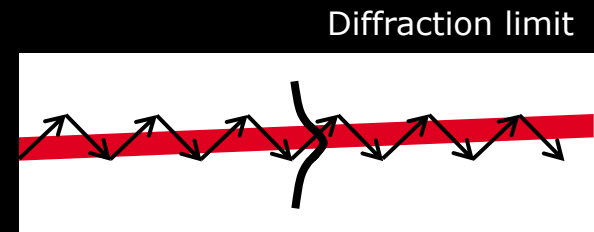
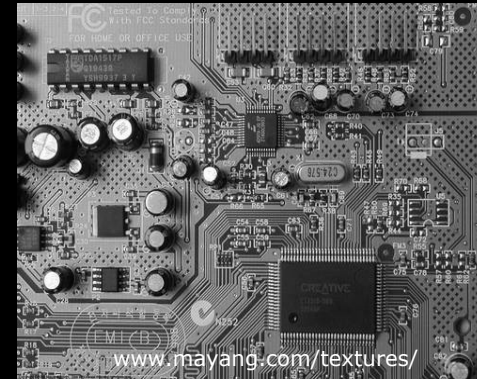
## HOW TO INTEGRATE ELECTRONICS AND OPTICS? SIZE MISMATCH...

### Electronic circuit

- + Very compact ( $< \sim 10\text{nm}$ )
- Operational speed is limited (RC-delay)

### Photonic circuit

- + High speed
- + High bandwidth
- Component size is limited ( $> \sim 1\ \mu\text{m}$ )



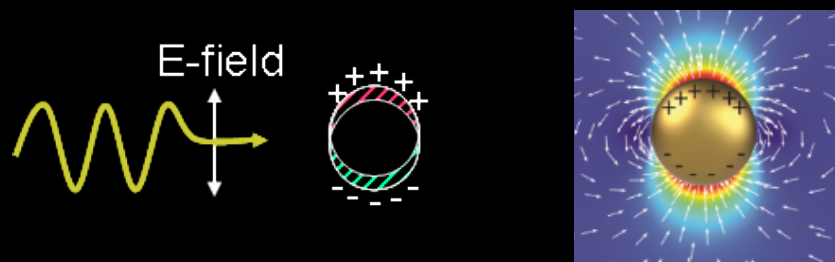
Optical mode in waveguide  $> \lambda_0/2n_{\text{CORE}}$

**SOLUTION: Optics on the Nanoscale**  
**PLASMONICS/ELECTRICAL METAMATERIALS**

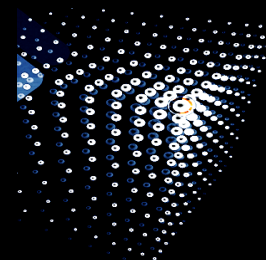
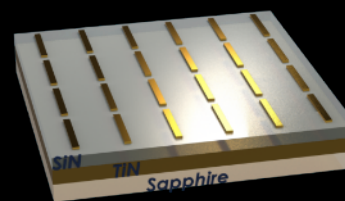
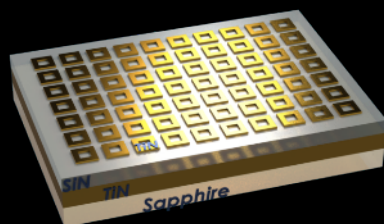


# PLASMONICS/(ELECTRICAL)METAMATERIALS

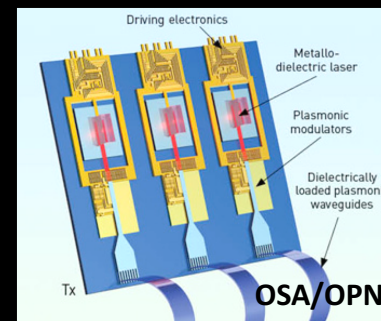
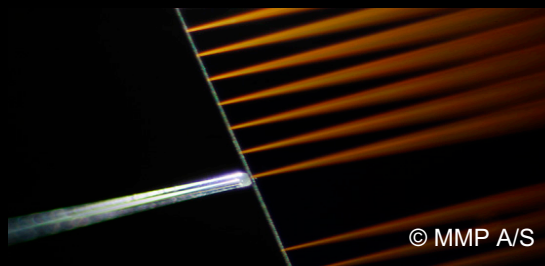
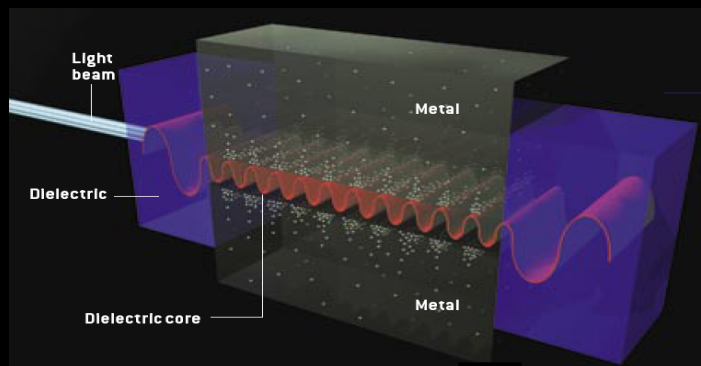
**1 Localized SP = Optical Nano-Antenna** (imaging, sensing, therapy, energy...)



= **Optical Metasurfaces** (ultra-thin/flat optics, sensors...)



**2 Propagating SP = Nano-Waveguide** (integrated photonics, lab-on-a-chip...)



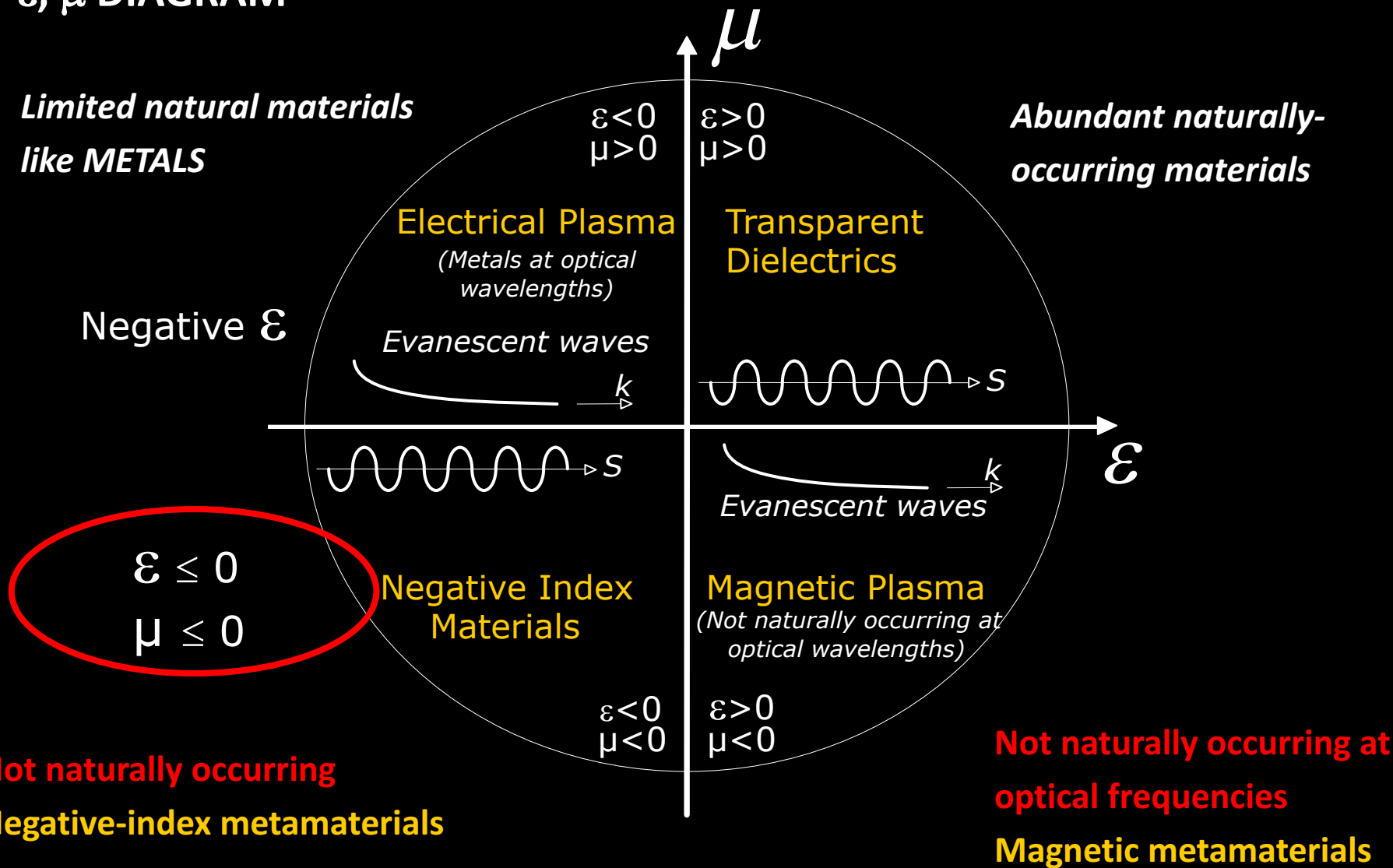
# Optical Negative-Index Metamaterials

# WHY WE NEED METAMATERIALS?

## $\epsilon, \mu$ DIAGRAM

Limited natural materials like METALS

Abundant naturally-occurring materials



# Negative refractive index: A historical review



Sir Arthur Schuster



Sir Horace Lamb

... energy can be carried forward at the group velocity but in a direction that is anti-parallel to the phase velocity...

Schuster, 1904

Negative refraction and backward propagation of waves

Mandel'stam, 1945



L. I. Mandel'stam



V. G. Veselago

Left-handed materials: the electrodynamics of substances with simultaneously negative values of  $\epsilon$  and  $\mu$

Veselago, 1968

Pendry, the one who whipped up the recent boom of NIM researches

Perfect lens (2000)

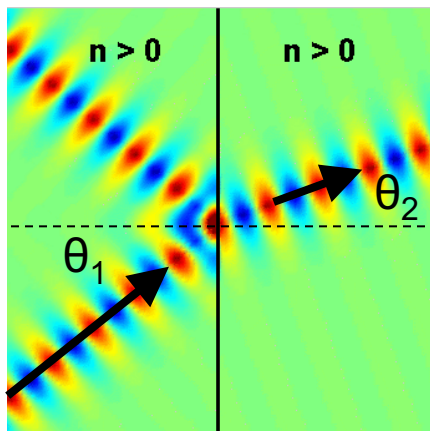
EM cloaking (2006)



Sir John Pendry

Others: Sivukhin. Agranovich,...

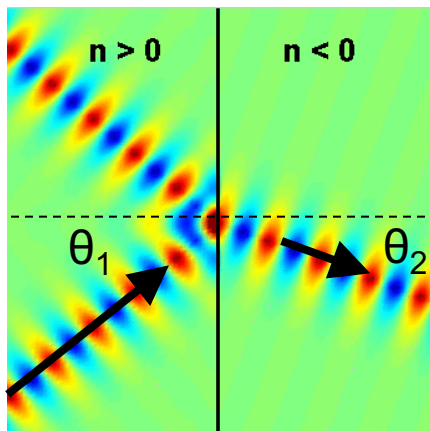
# Metamaterials with Negative Refraction



- Refraction:  $n^2 = \epsilon\mu$   
 $n = \pm\sqrt{\epsilon\mu}$

- Figure of merit:  $F = |n'| / n''$

$$n < 0, \text{ if } \epsilon'|\mu| + \mu'|\epsilon| < 0$$

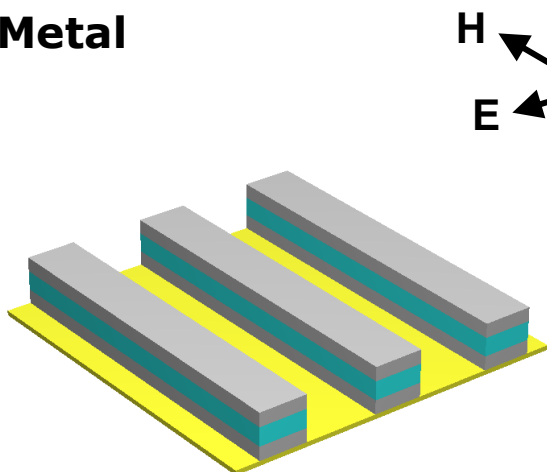


# Negative Permeability and Negative Permittivity

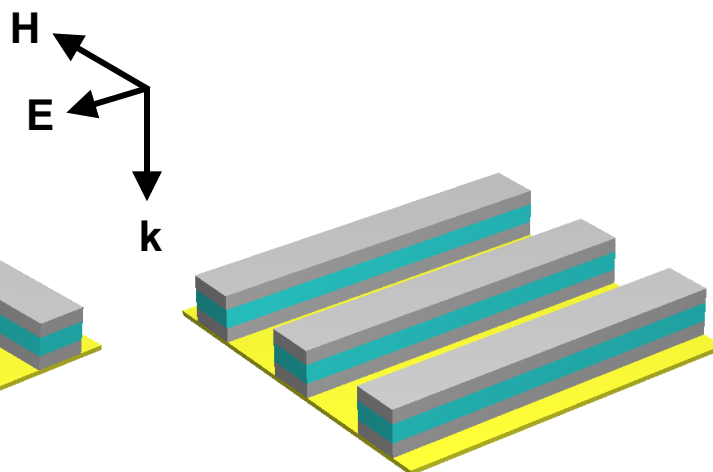
S. Zhang, et al., PRL (2005)

■ Dielectric

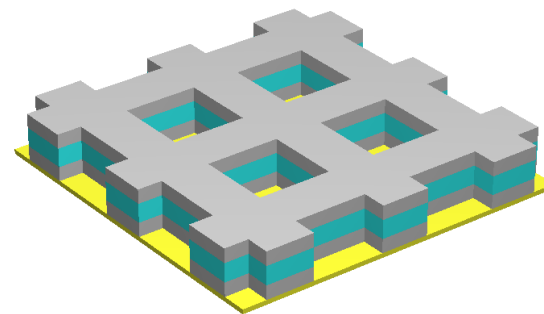
■ Metal



**Nanostrip pair (TM)**  
 $\mu < 0$  (resonant)

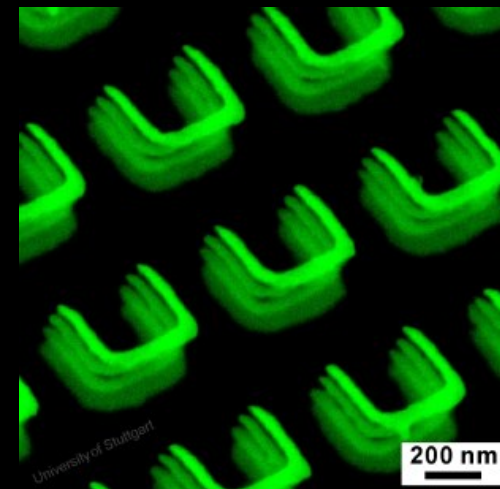
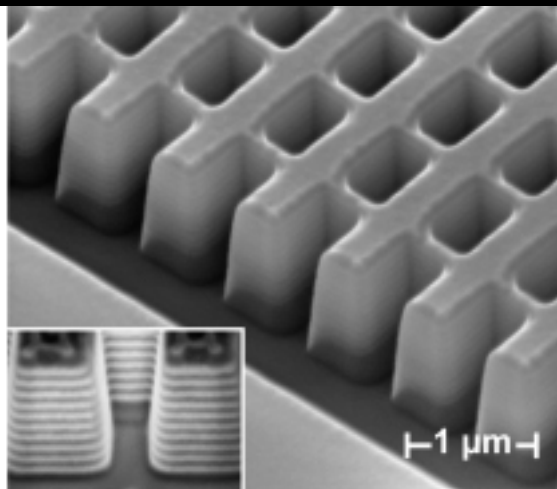
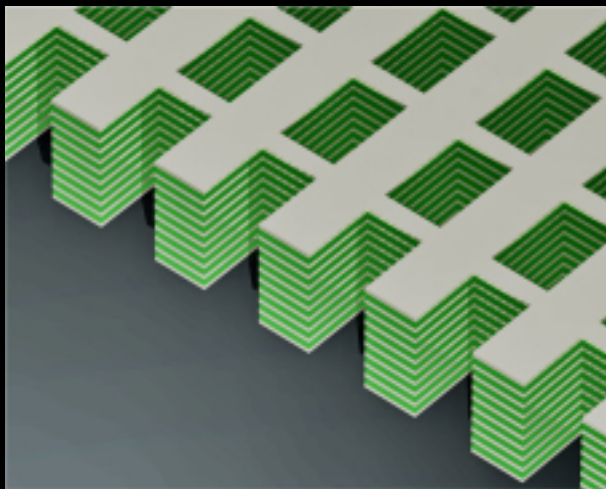
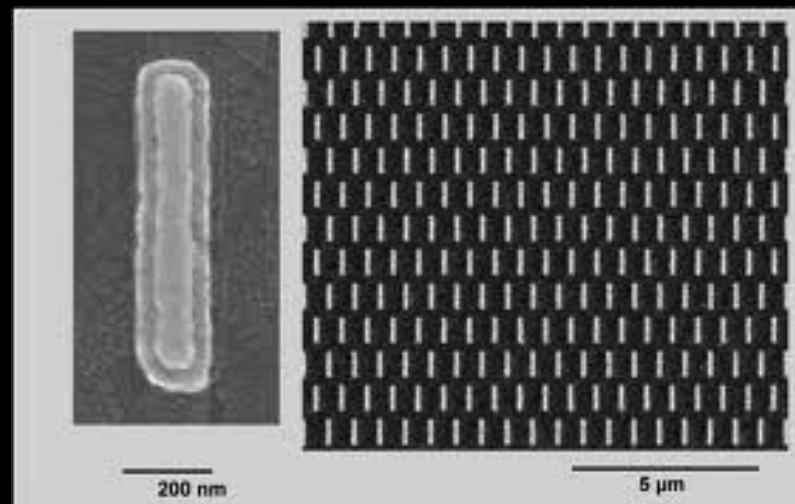
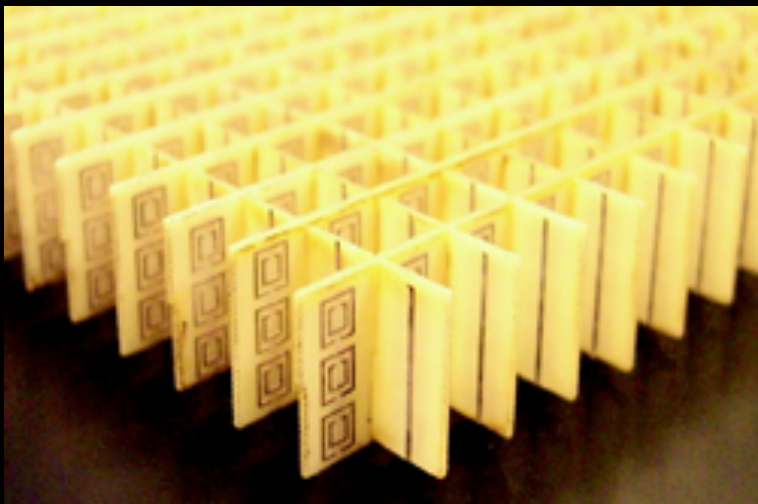


**Nanostrip pair (TE)**  
 $\epsilon < 0$  (non-resonant)



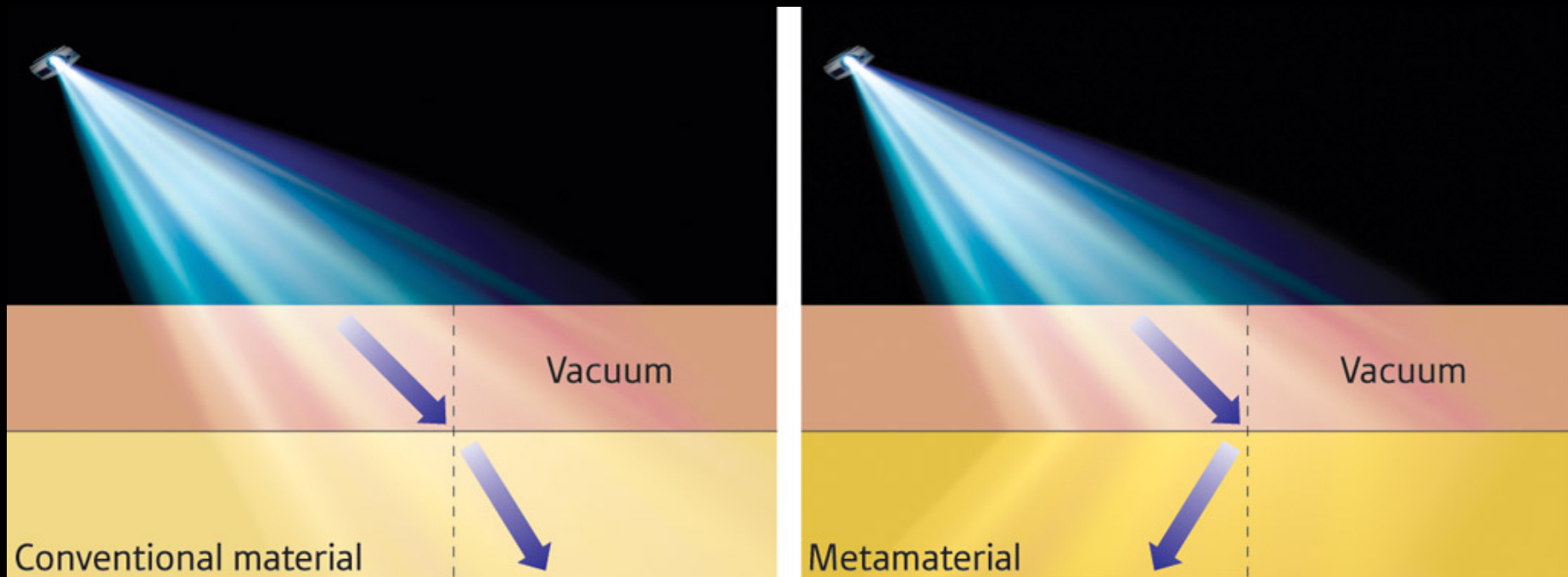
**Fishnet**  
 $\epsilon$  and  $\mu < 0$

# NEGATIVE INDEX MMs



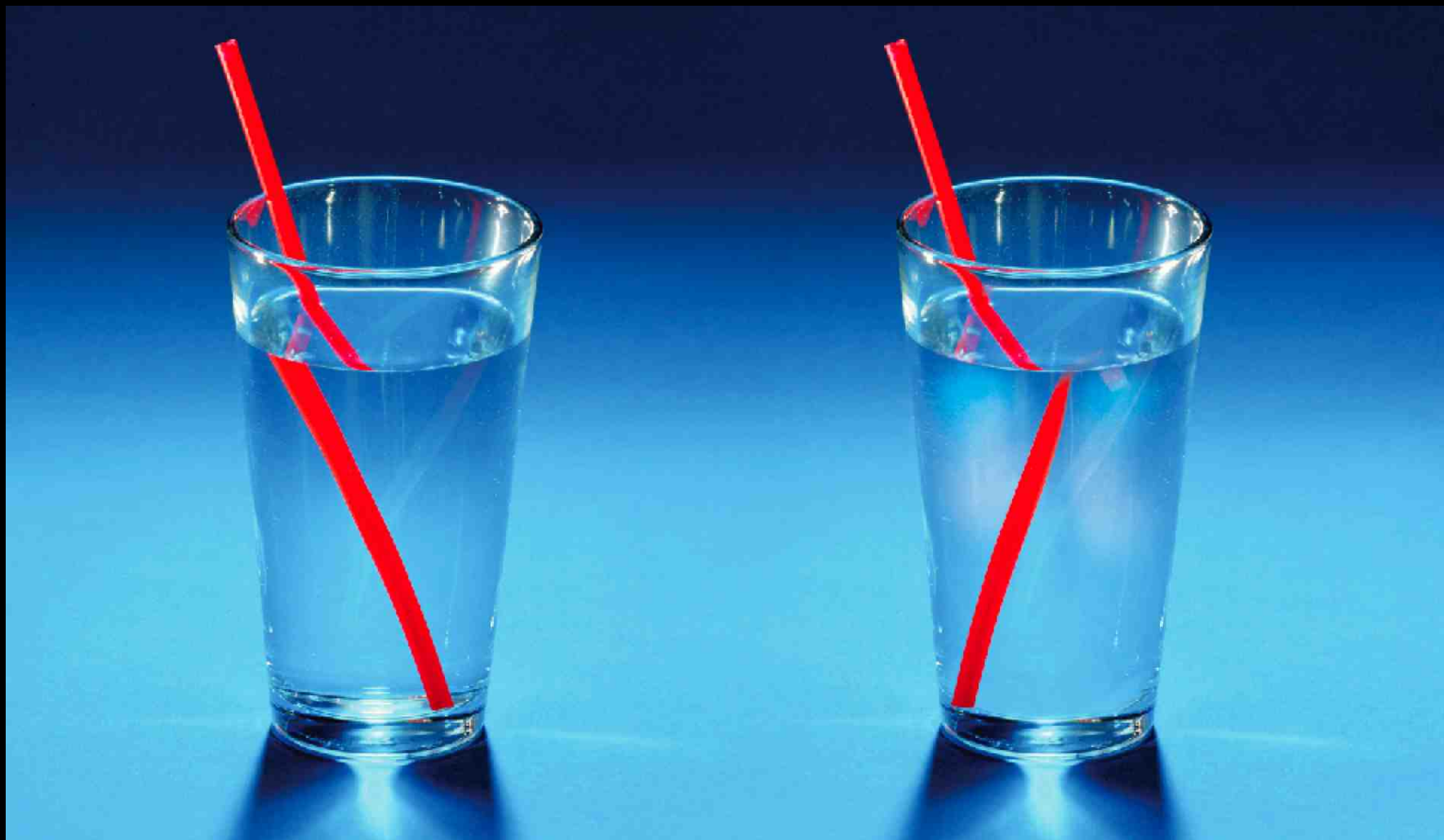
# NEGATIVE REFRACTION EFFECTS

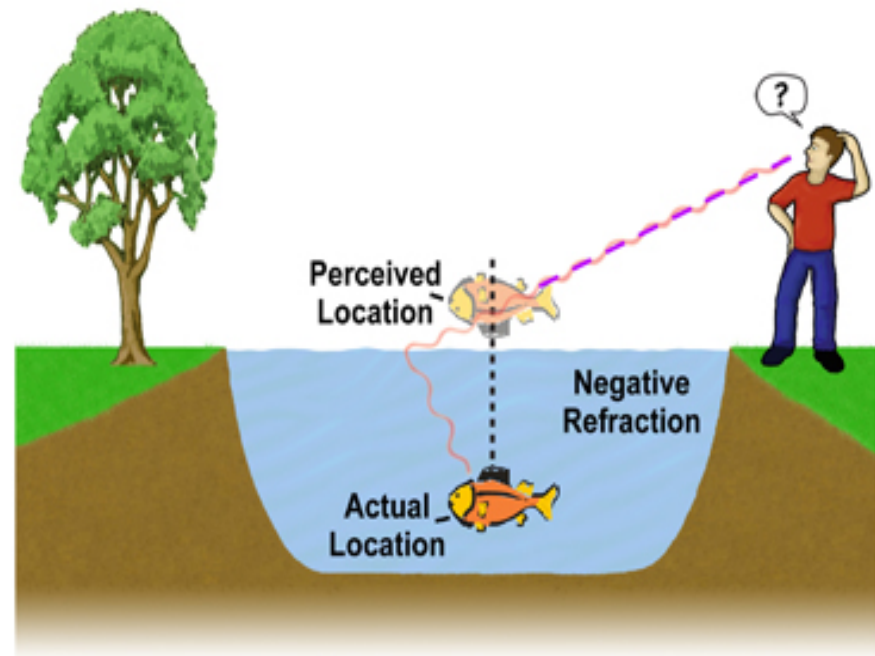
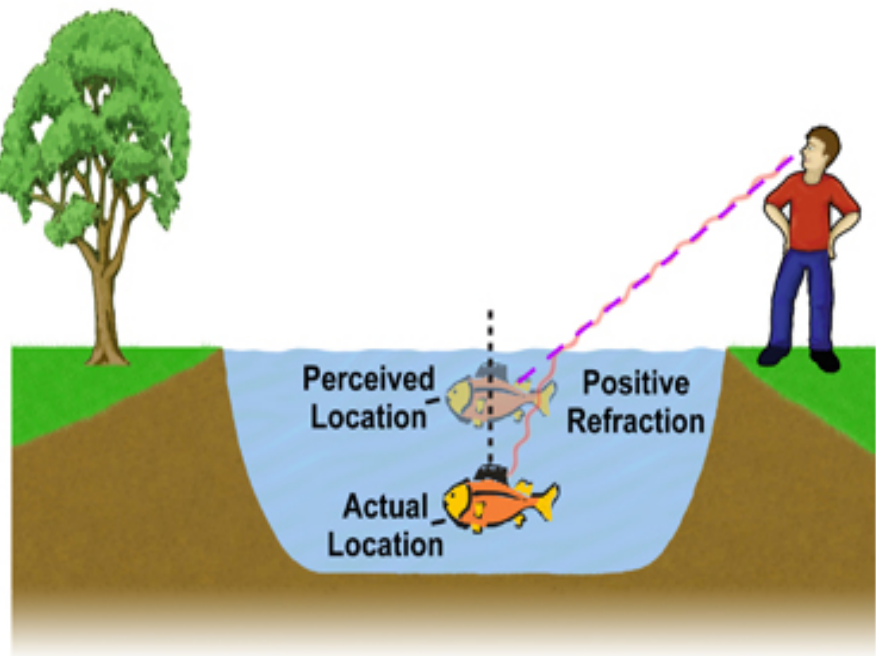
In normal materials, light cannot bend beyond the perpendicular to the interface but in Metamaterials it can.





# NEGATIVE REFRACTION EFFECTS

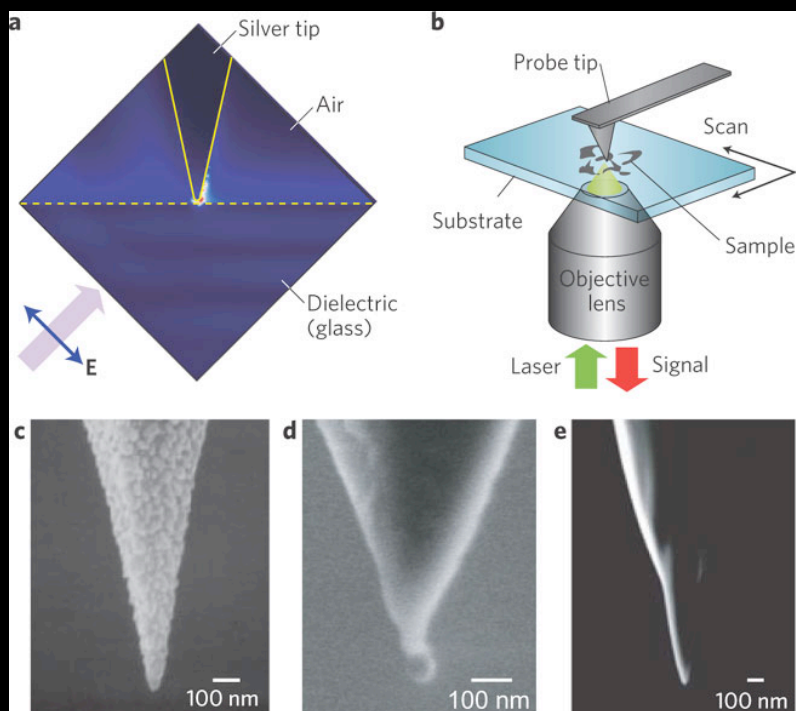




# WHAT WE HAVE SO FAR

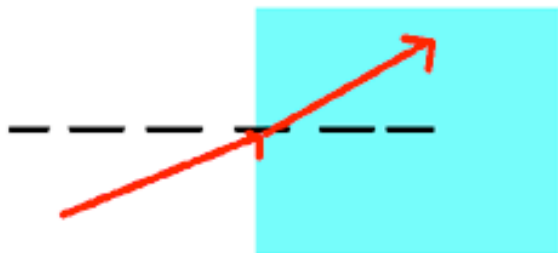
The diffraction limit is an inherent limitation in conventional optical devices or lenses:  
Optical microscope resolves features down to  $\sim 200\text{nm}$

Nanoprobes are needed to go to the nanoscale...



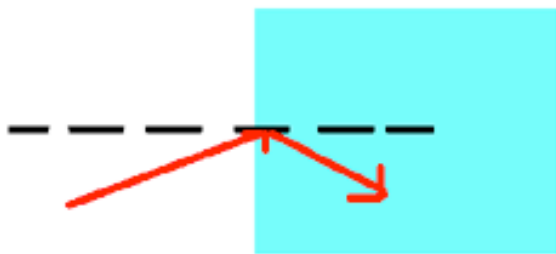
# SUPERLENS: SEEING ON NANOSCALE

a)



positive refractive index material

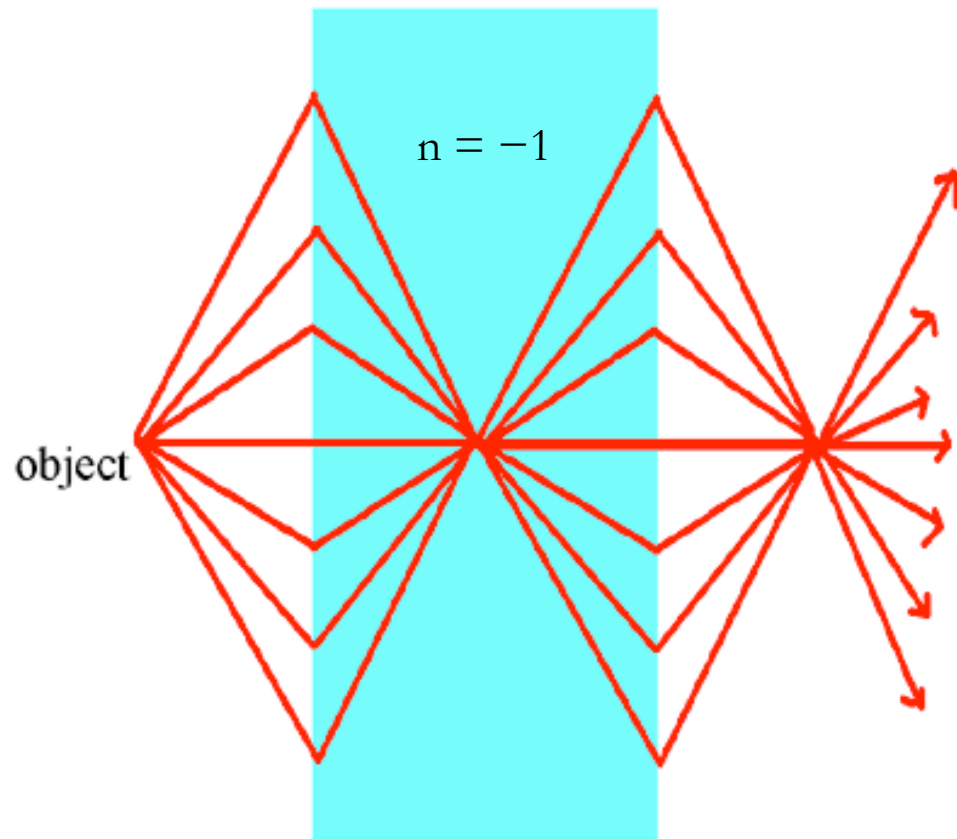
b)



negative refractive index material

c)

Negative refraction re-focuses waves  
Allows subwavelength imaging



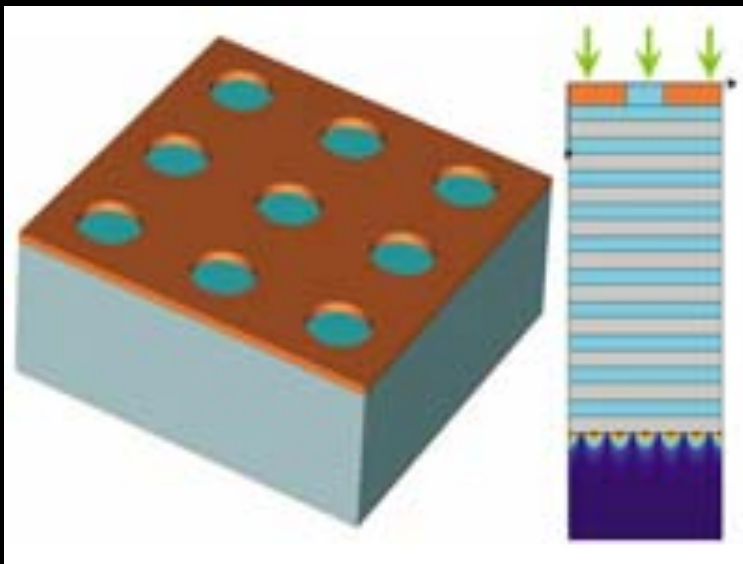
# TECHNOLOGY/ECONOMY IMPACT

Superlens uses metamaterials to go **beyond the diffraction limit**

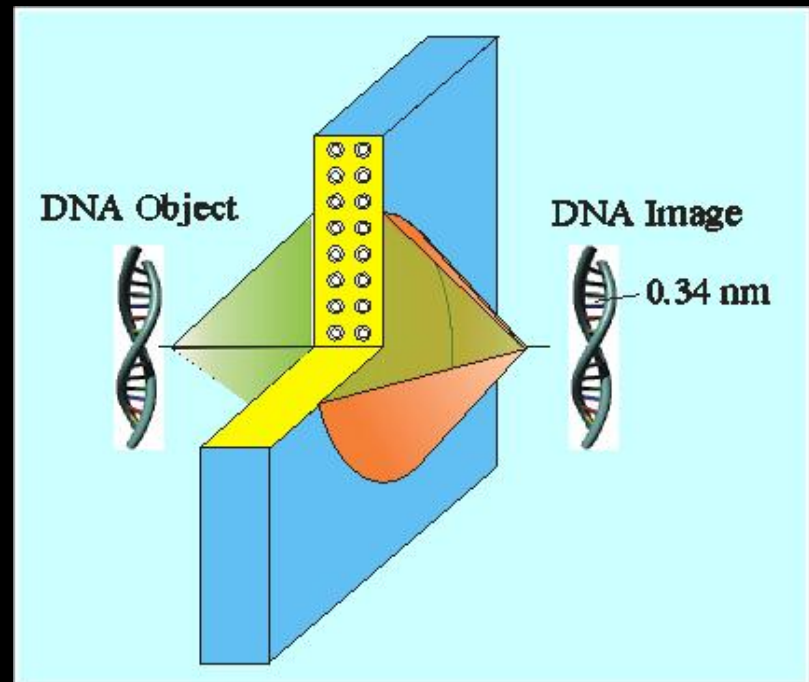
*Seeing on the nanoscale*

Next Generation of Imaging Systems

Next Generation of Nanolithography Tools

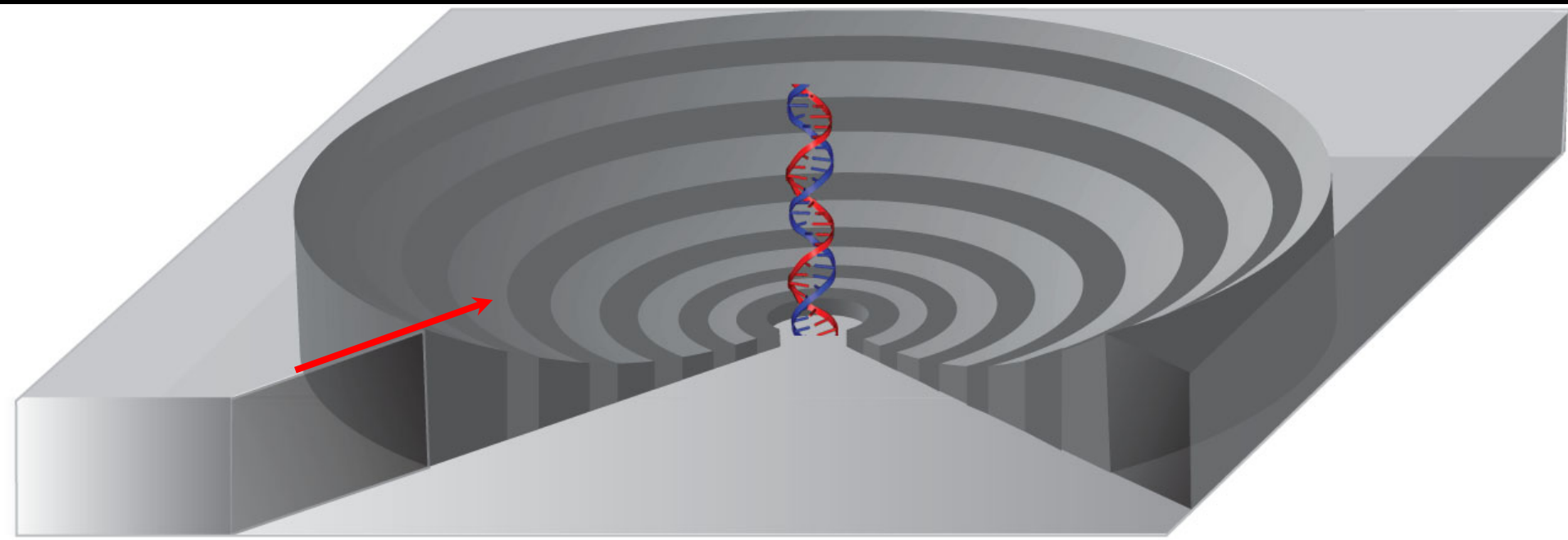


Group of Z. Liu



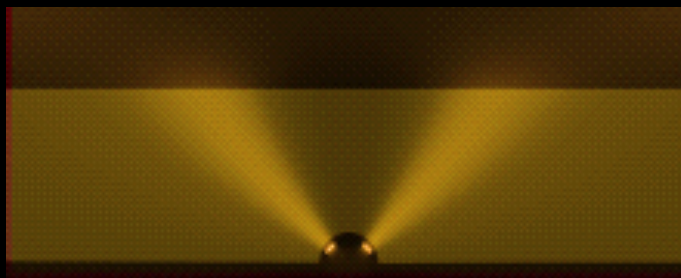
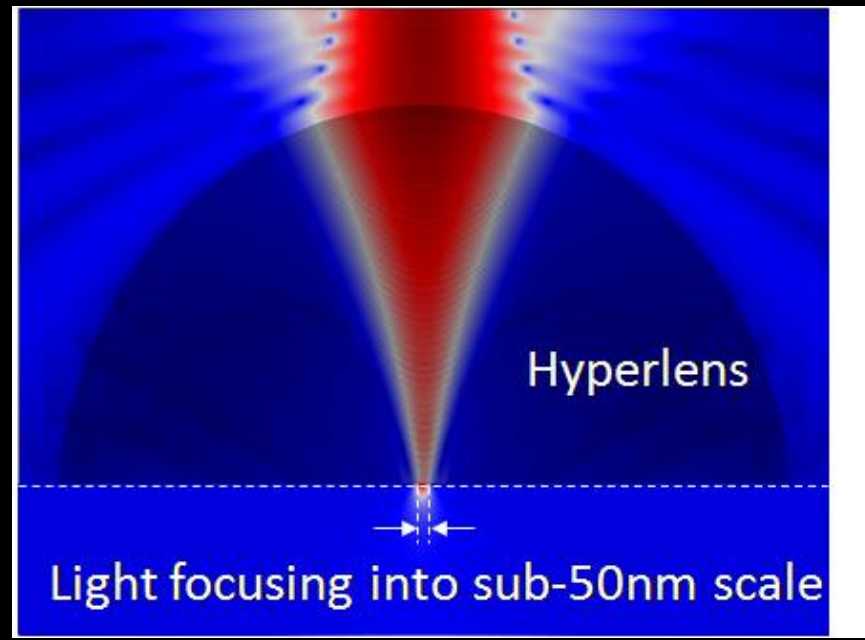
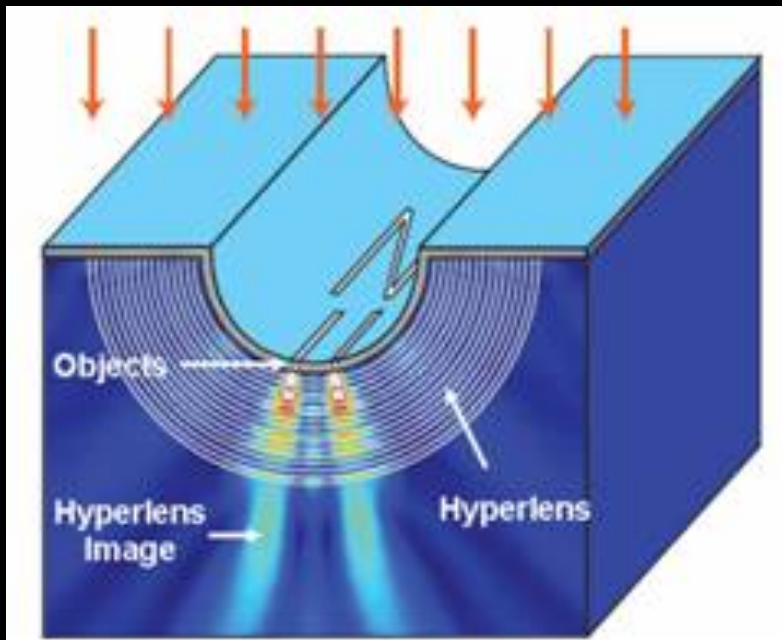
# HYPERLENS

Magnifying Hyperlens:  
Resolving nanometer scale features

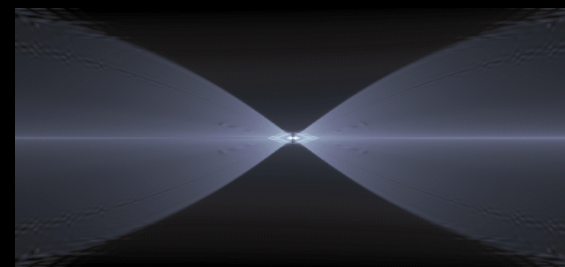


Far-field sub- $\lambda$  imaging

# HYPERLENS



**Magnifying hyperlens**



**Light concentrator**



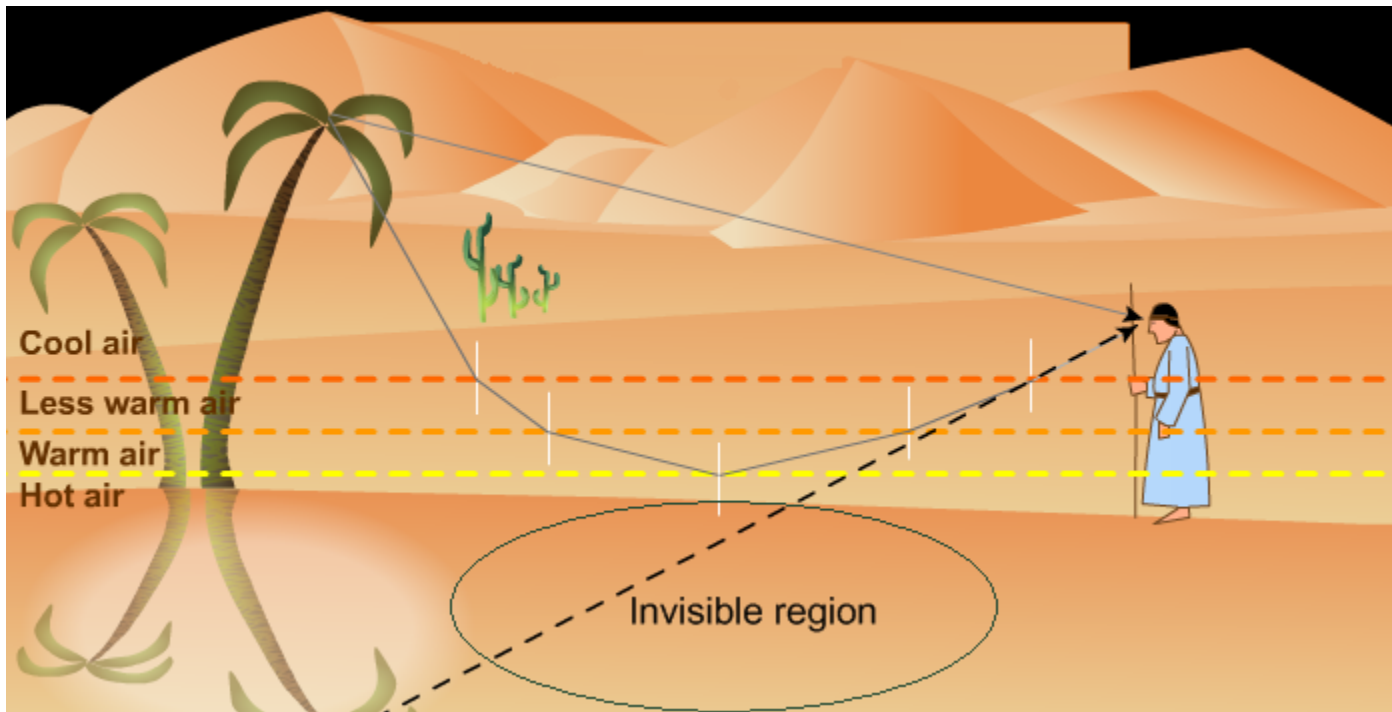
# **Transformation Optics: Optical Cloaking & Trapped Rainbow**





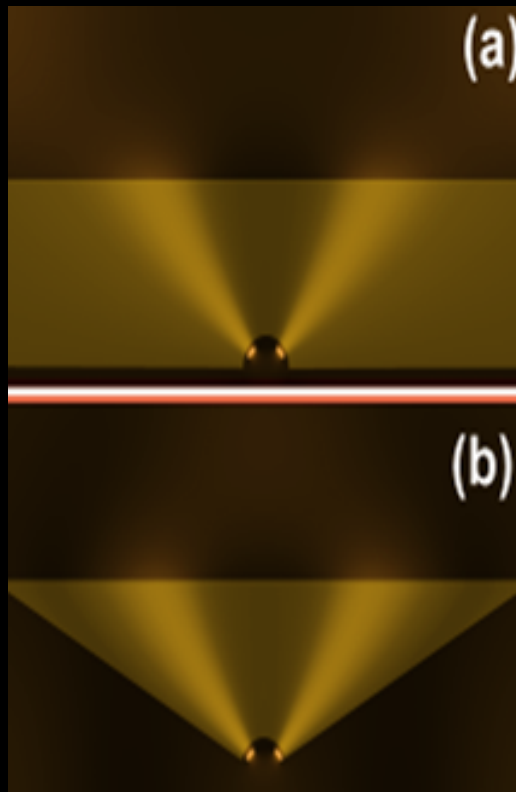
# A similarity in Mother Nature

The bending of light due to the gradient in refractive index in a **desert mirage**



# Engineering Meta-Space for Light via Transformation Optics

Kildishev, VMS (*OL*, 2008); Shalaev, *Science* 322, 384 (2008)

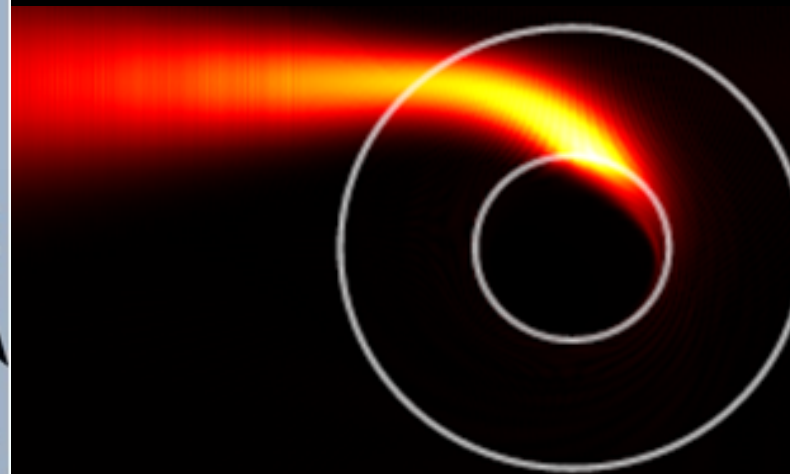


Planar hyperlens  
(Kildishev and VMS)  
(Schurig et al; Zhang group)



Light concentrator  
(also, Schurig et al)

*Fermat:*  $\delta \int n dl = 0$   
 $n = \sqrt{\epsilon(r)\mu(r)}$   
*curving optical space*



Optical Black Hole  
(Zhang group;  
Narimanov, Kildishev)

# Form-invariance of Maxwell's equations

Coordinate transformation from  $\mathbf{X}$  to coordinate  $\mathbf{X}'$  is described using the Jacobian matrix  $\mathbf{G}$ :

$$g_{ij} = \partial x'_i / \partial x_j$$

Maxwell's equation in  $\mathbf{x}$

$$\nabla \cdot (\varepsilon \vec{E}) = \rho$$

$$\nabla \cdot (\mu \vec{H}) = 0$$

$$\nabla \times \vec{E} = -\mu \frac{\partial \vec{H}}{\partial t}$$

$$\nabla \times \vec{H} = \varepsilon \frac{\partial \vec{E}}{\partial t} + \vec{J}$$

Transformation of variables

$$\varepsilon' = \frac{G \varepsilon G^T}{|G|}; \quad \mu' = \frac{G \mu G^T}{|G|}$$

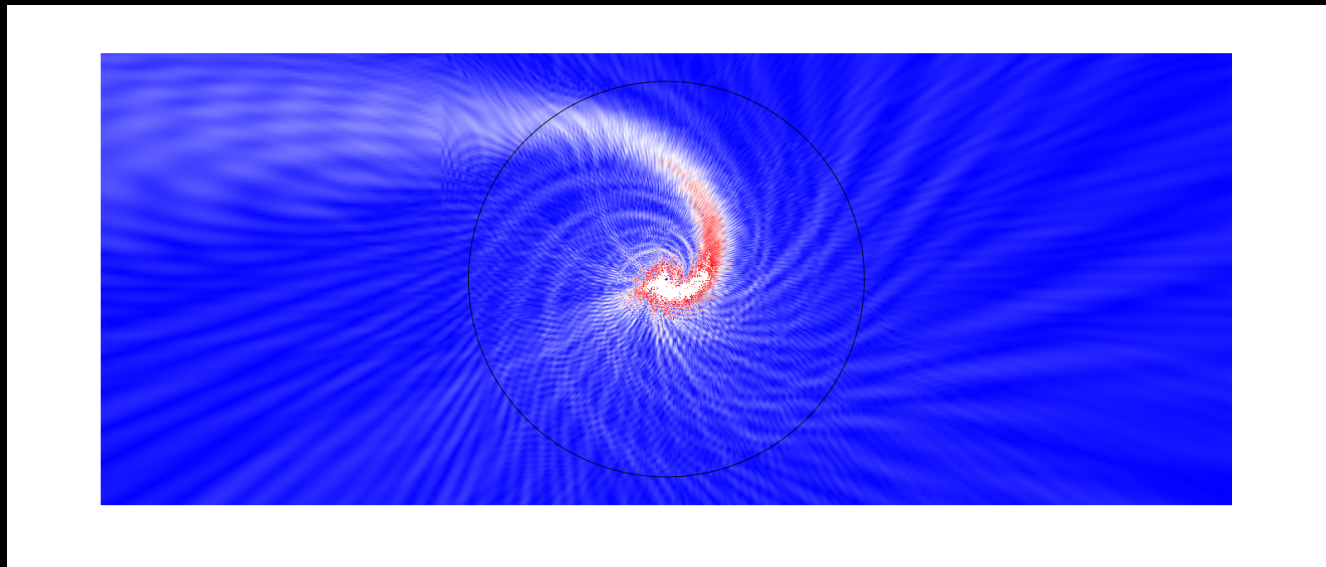
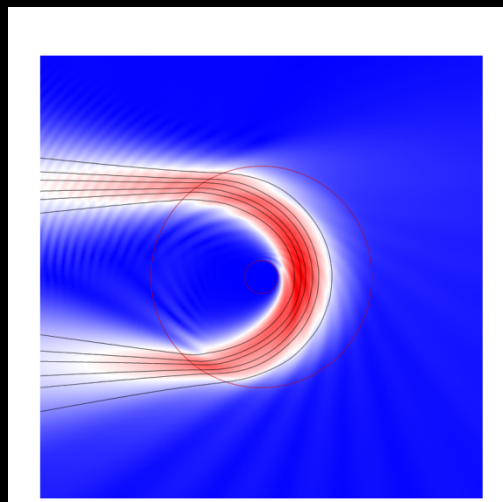
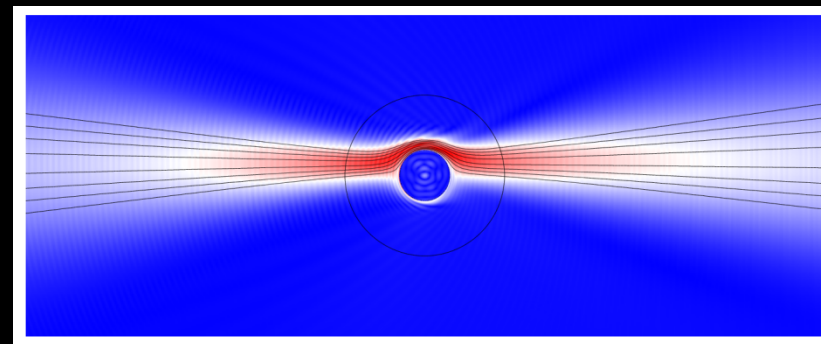
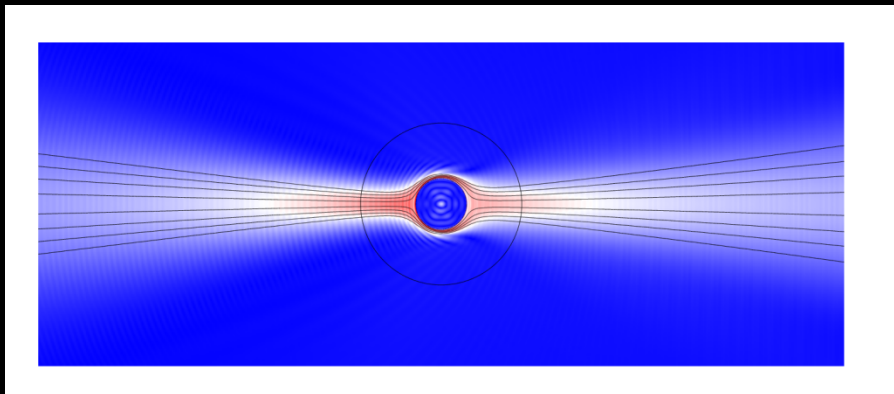
$$\vec{E}' = (G^T)^{-1} \vec{E}; \quad \vec{H}' = (G^T)^{-1} \vec{H}$$

$$\vec{J}' = \frac{G \vec{J}}{|G|}; \quad \rho' = \frac{\rho}{|G|}$$

$$\nabla \rightarrow \nabla'$$

# Trapping and Manipulating Light

Narimanov, Kildishev



# Invisibility in Nature, Physics and Technology

- Natural camouflage
- Black hole
- ...

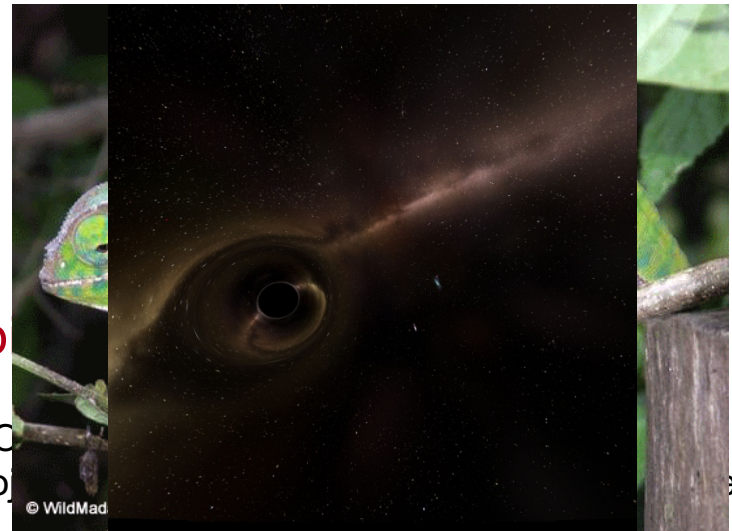
## Current technologies to achieve invisibility

- Stealth technique:  
Radar cross-section reductions by absorbing paint / non-metallic frame / shape effect...



F-117 "Nighthawk" Stealth Fighter

- Cloaking Project



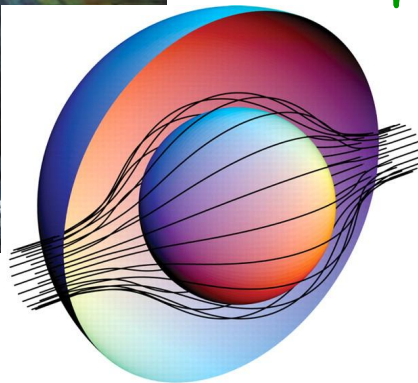
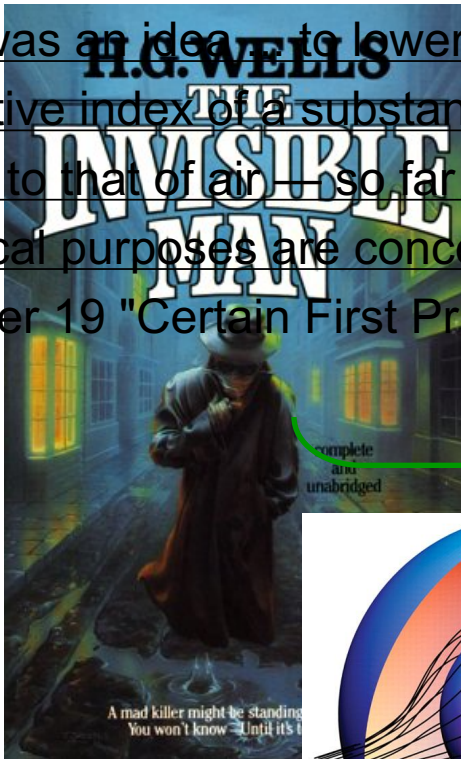
Optical Camouflage, Tachi Lab, U. of Tokyo, Japan

# Invisibility: from fiction to fact?

## Examples with scientific elements:

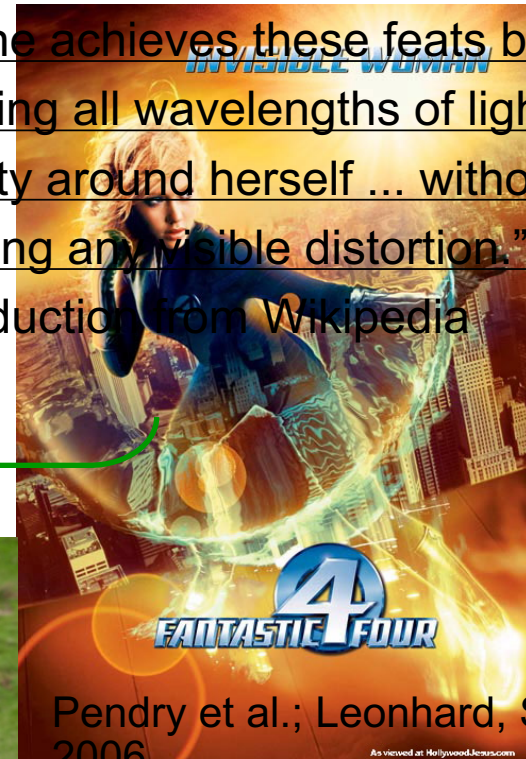
- The Invisible Man by H. G. Wells (1897)

"... it was an idea ... to lower the refractive index of a substance, solid or liquid, to that of air — so far as all practical purposes are concerned." -- Chapter 19 "Certain First Principles"



- "The invisible woman" in The Fantastic 4 by Lee & Kirby (1961)

"... she achieves these feats by bending all wavelengths of light in the vicinity around herself ... without causing any visible distortion." -- Introduction from Wikipedia

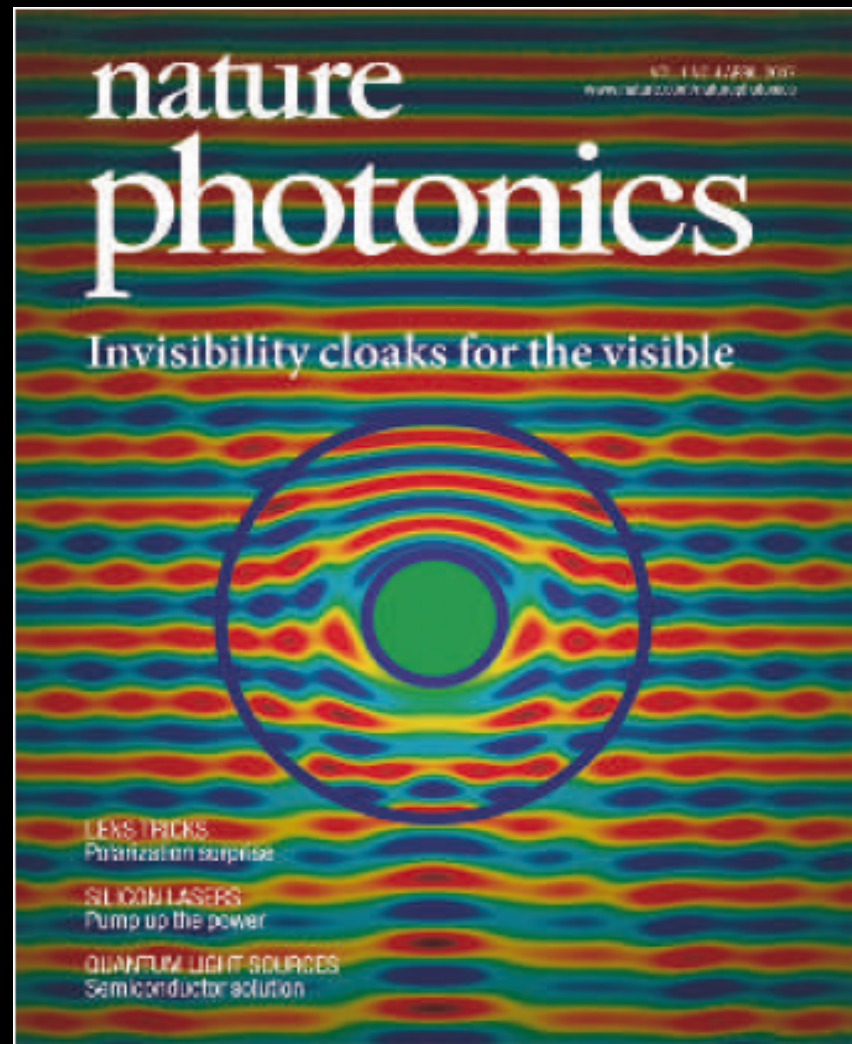
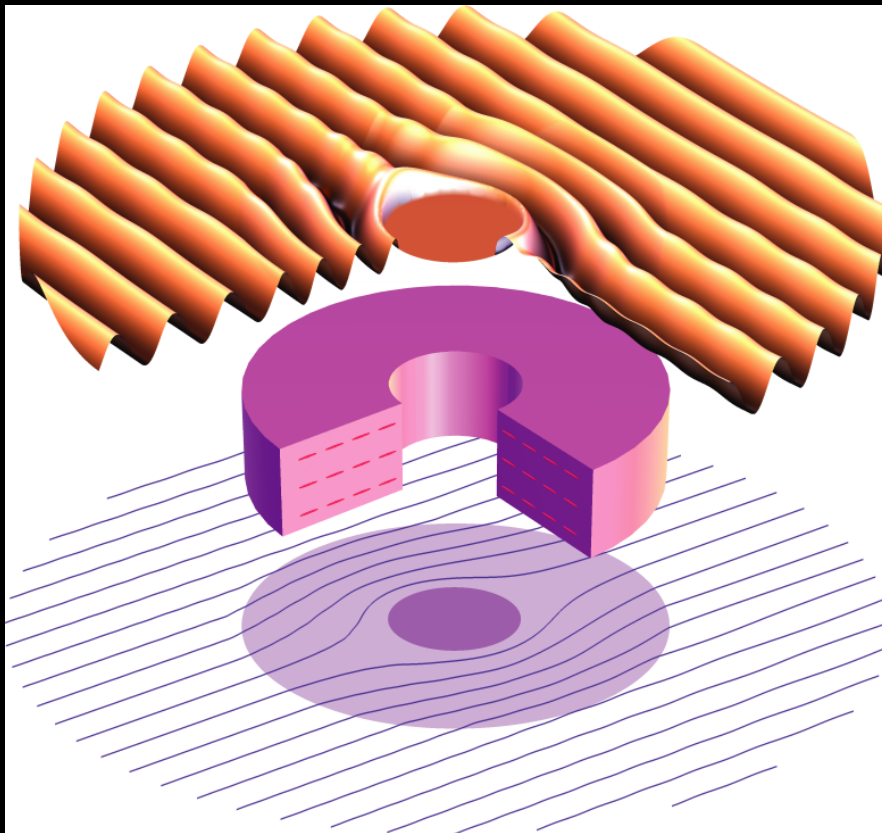


Pendry et al.; Leonhard, Science, 2006

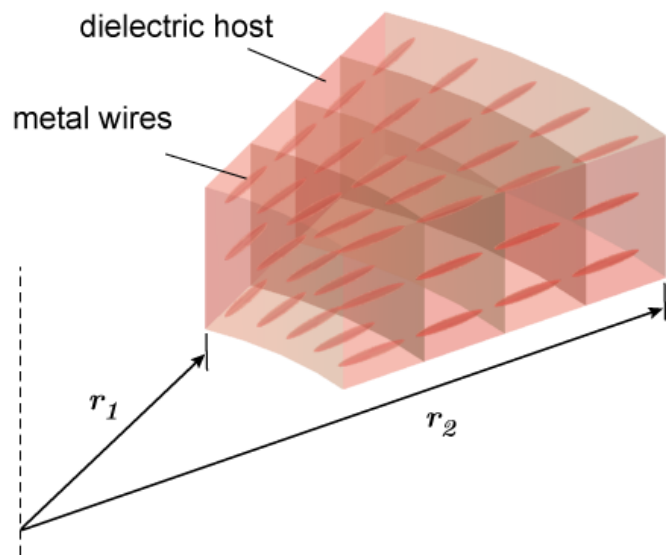
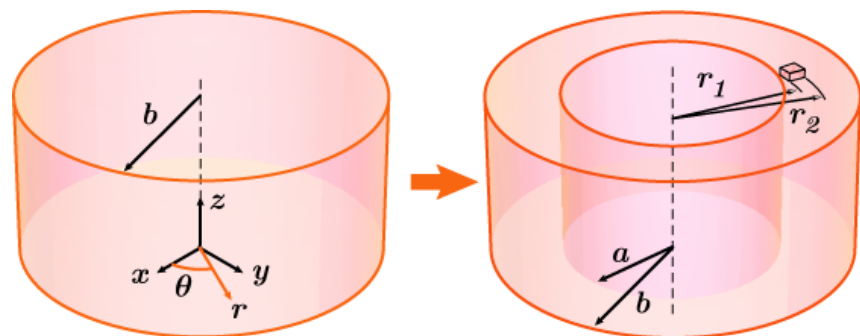
(Earlier work: cloak of thermal conductivity by Greenleaf et al., 2003)



# Optical Cloaking with Metamaterials: Can Objects be Invisible in the Visible?

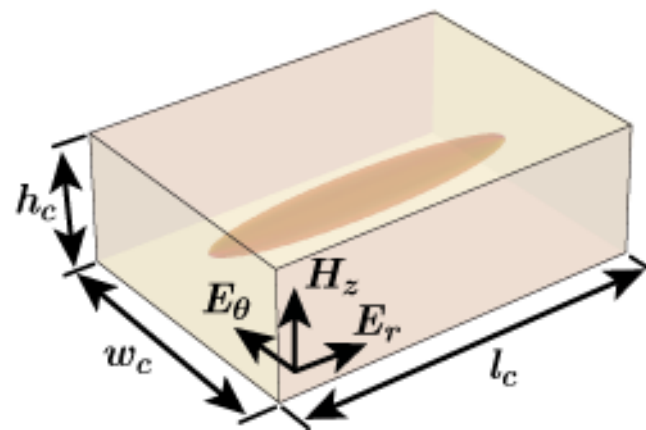


# Structure of the cloak: "Round brush"



metal needles embedded in dielectric host

Unit cell:

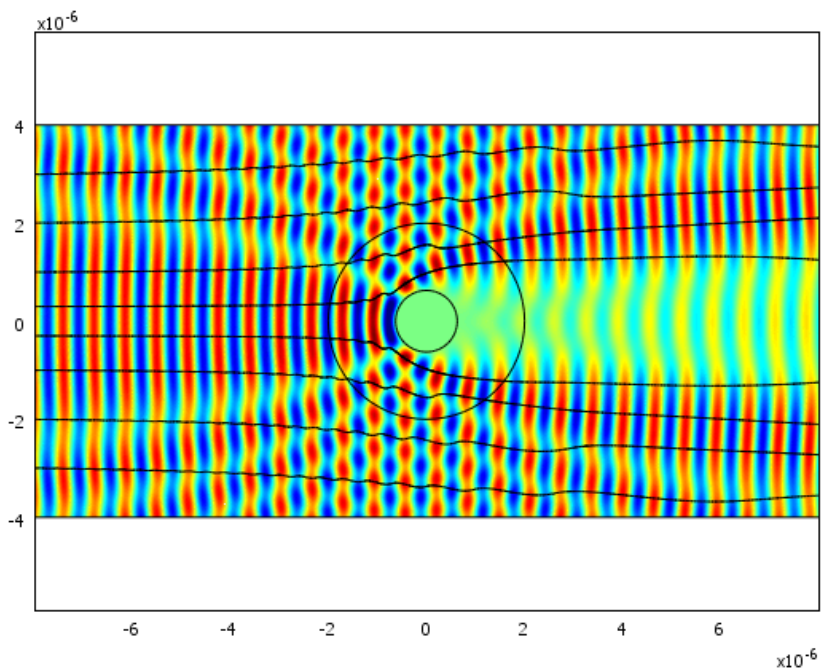


Flexible control of  $\epsilon_r$  ;  
Negligible perturbation in  $\epsilon_\theta$

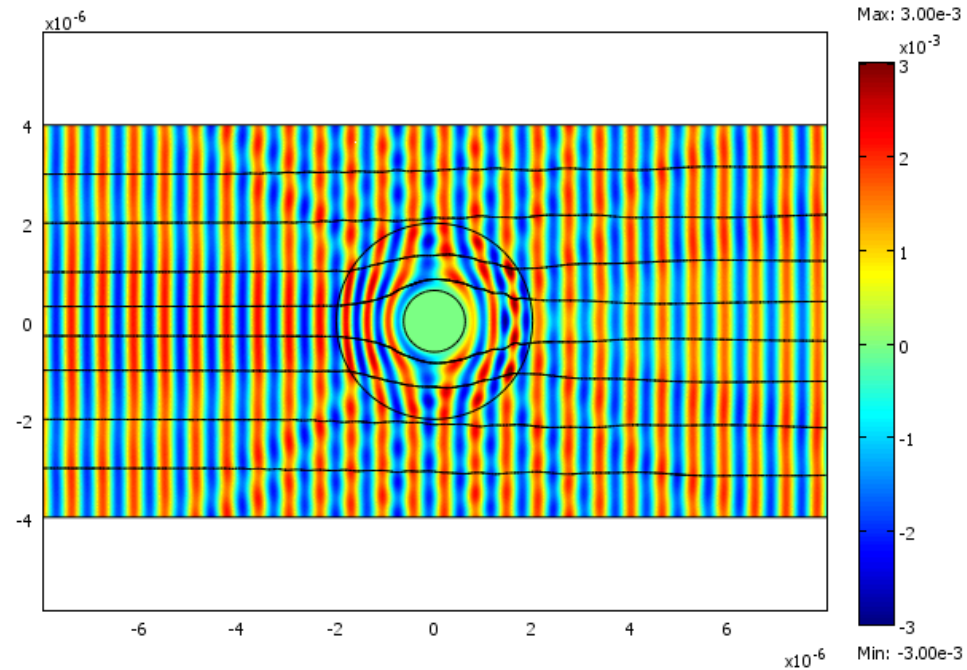


# Cloaking performance: Field mapping movies

Example: cloak @ 632.8nm with silver wires in silica

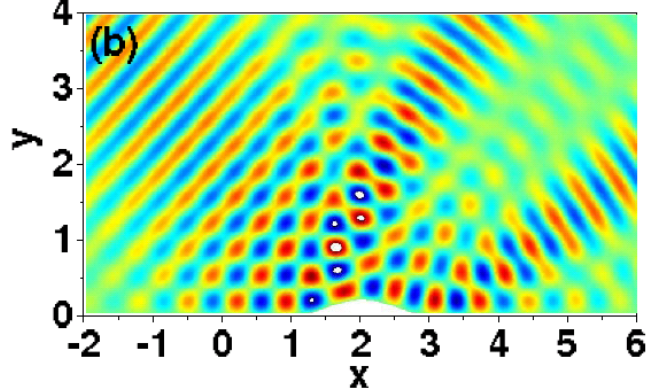
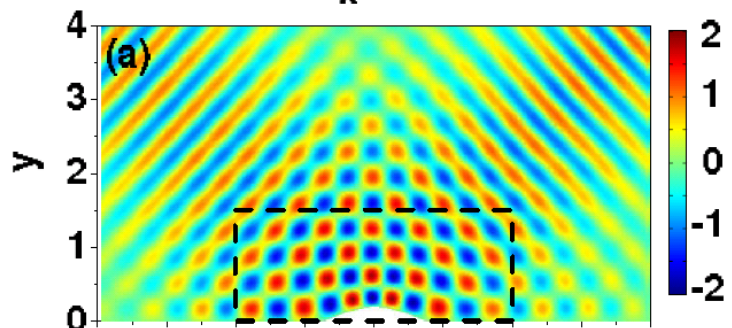
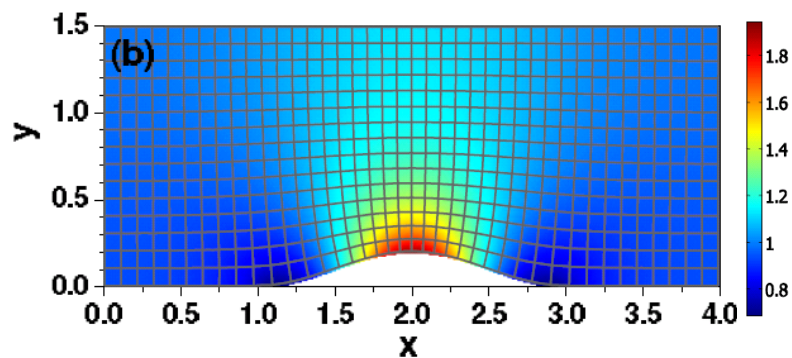


Cloak OFF



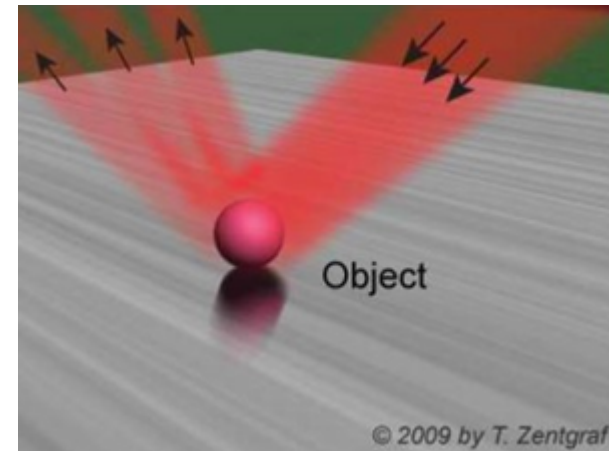
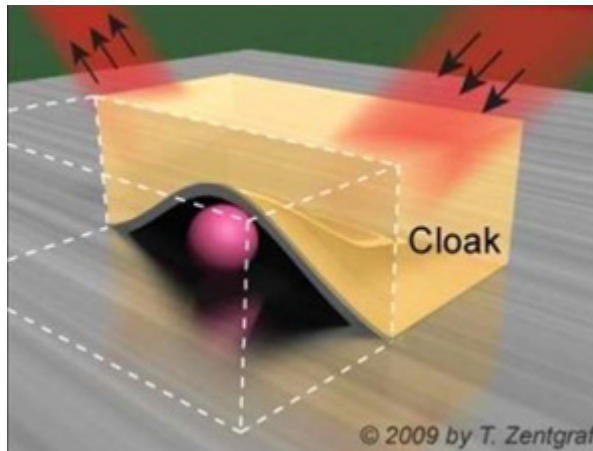
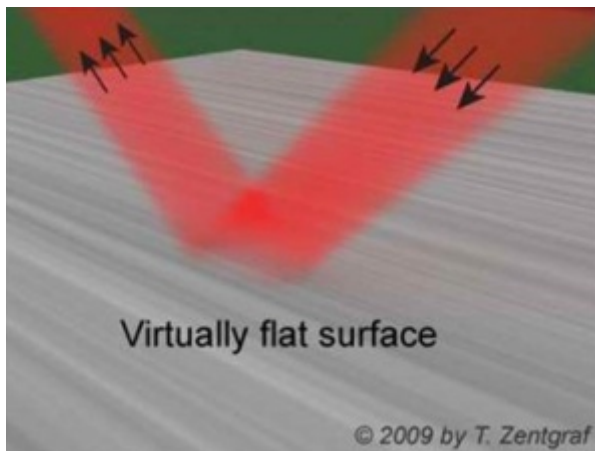
Cloak ON

# Invisible Carpet (ground-plane cloak)

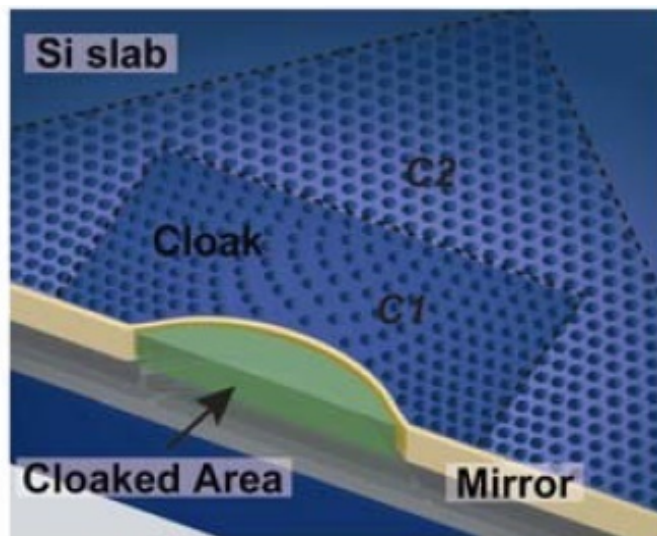


picture from discovery.com

# Optical Mimicry

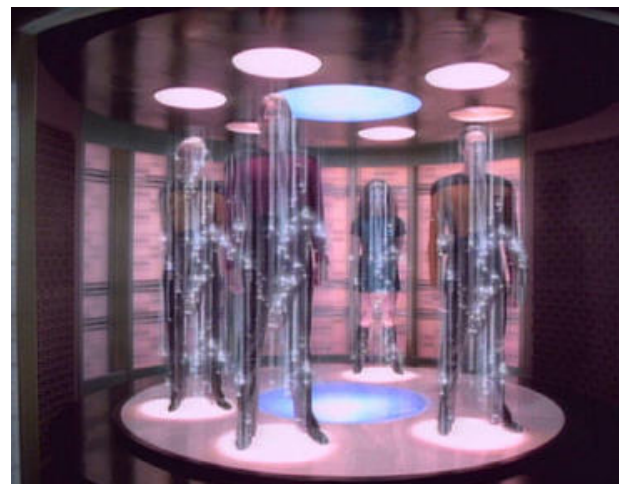
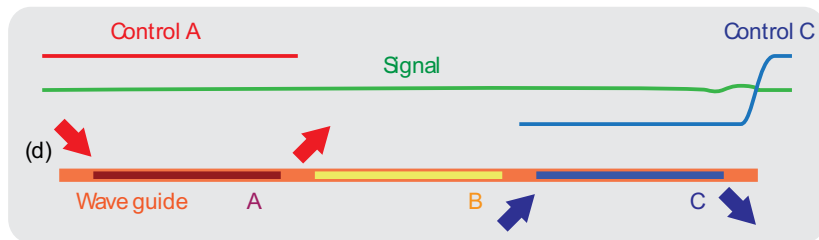
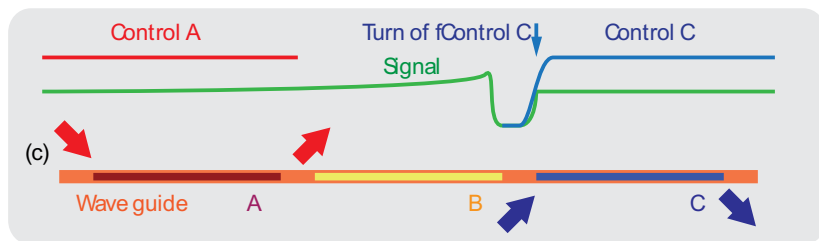
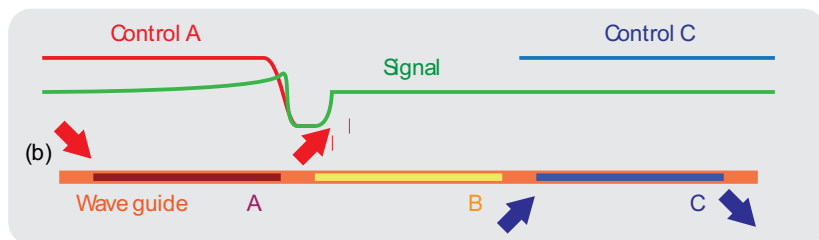
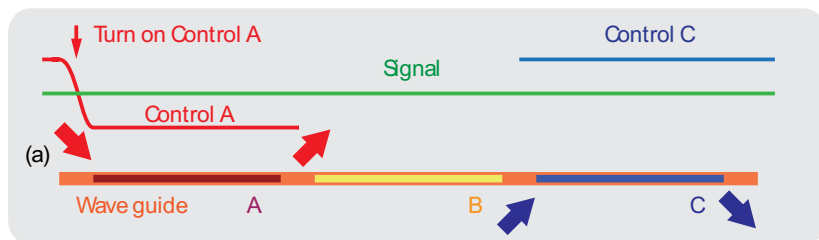


Progress Towards True Invisibility on May.17, 2009, under Science  
[www.codingfuture.com](http://www.codingfuture.com)

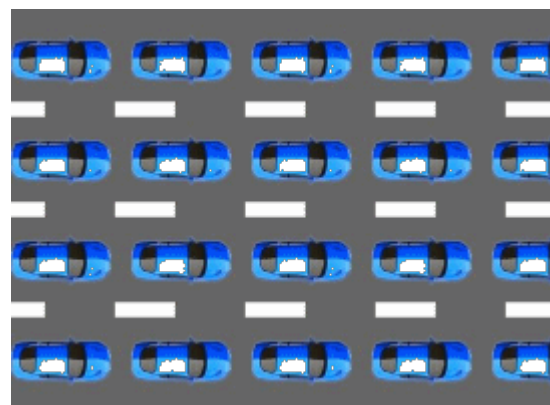


Theory: J. Li, J. Pendry  
 GHz: Smith et al (Duke)  
 Optical: Zhang et al (Berkeley)  
 Lipson et al (Cornel)

# Space-time Cloak – History Editor



Star Trek transporter

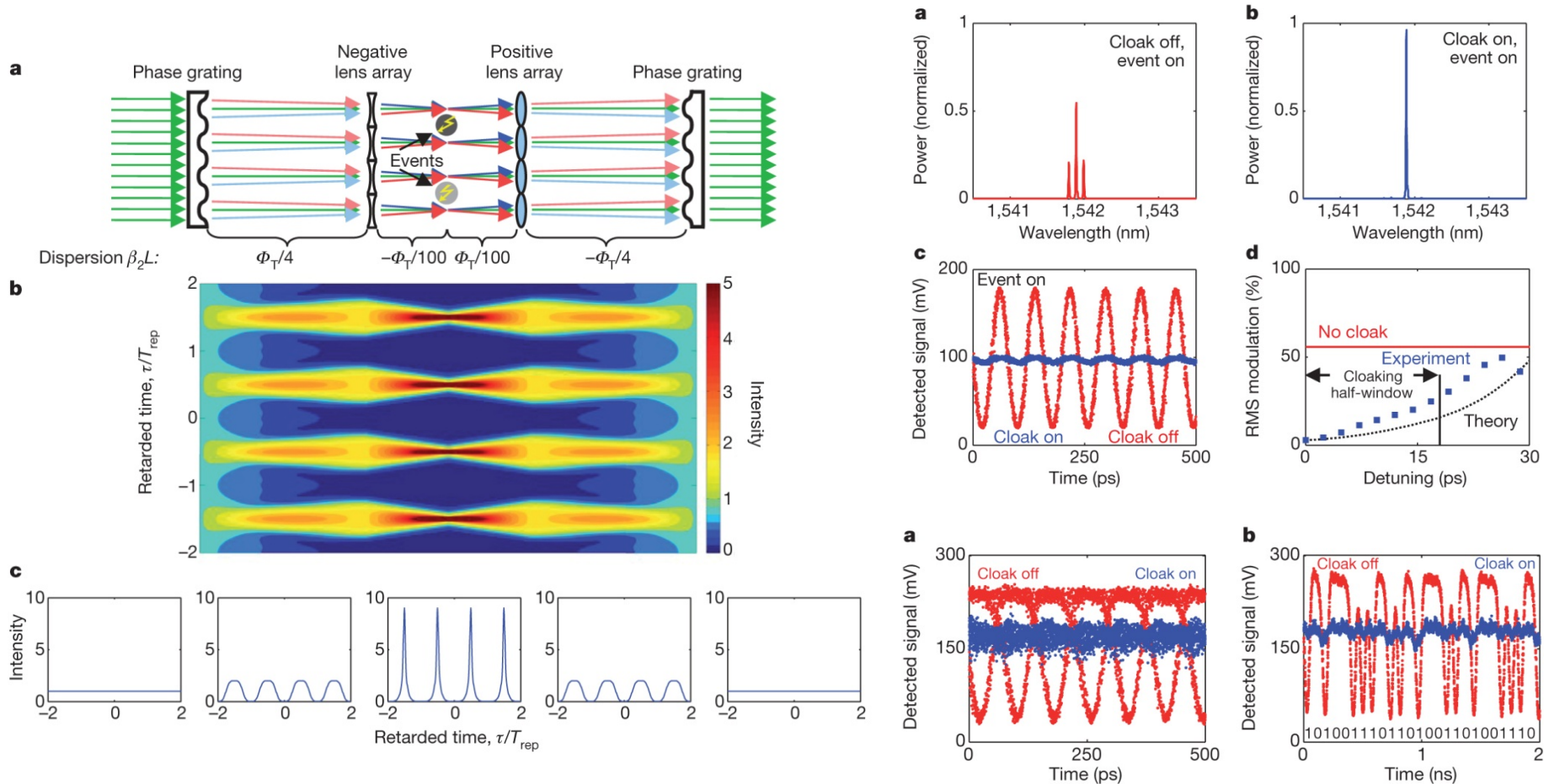


M. W. McCall and et al., *Journal of Optics*, 2011  
Gaeta et al, experiment

# A temporal cloak at telecommunication data rate

Jun. 13 2013 • Vol 498, Issue 7453

Joseph M. Lukens, Daniel E. Leaird & Andrew M. Weiner

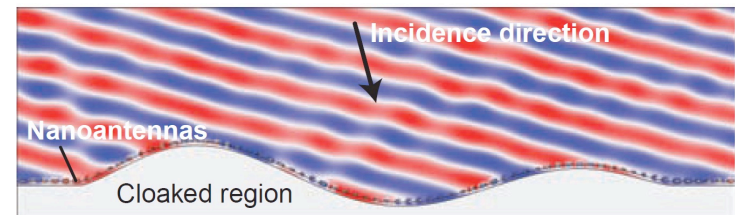
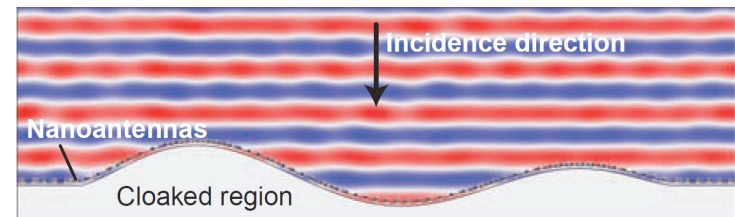
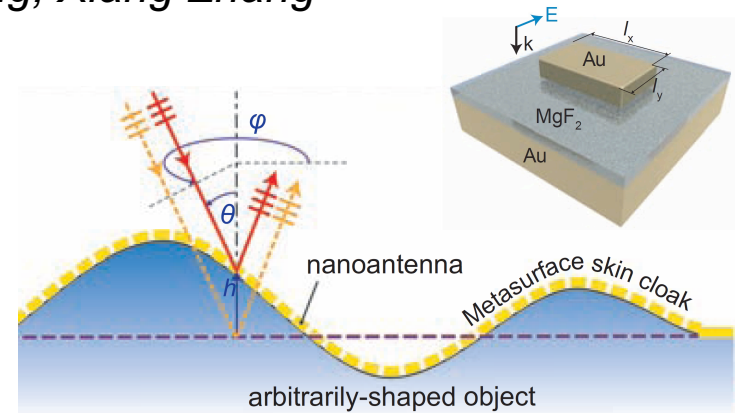
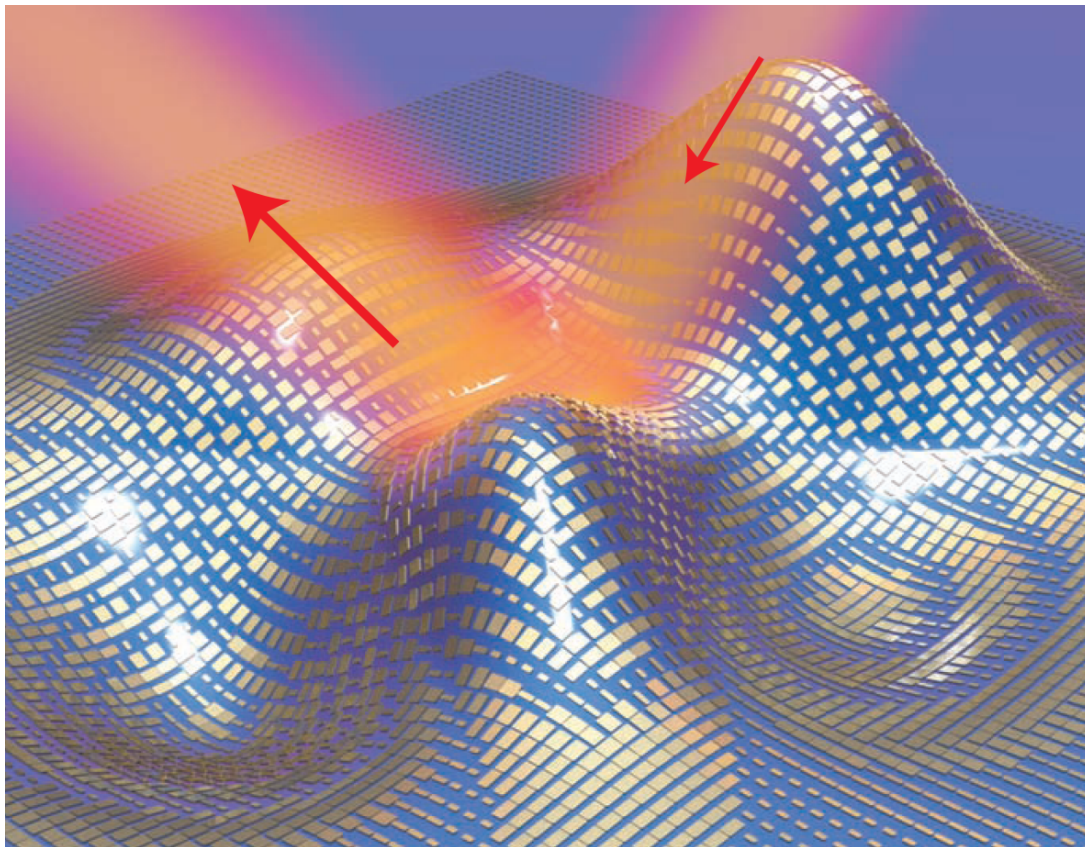


Similar work: "Fridman, M., Farsi, A., Okawachi, Y. & Gaeta, A. L. *Nature* 481, 62–65 (2012)"

# An ultrathin invisibility skin cloak for visible light

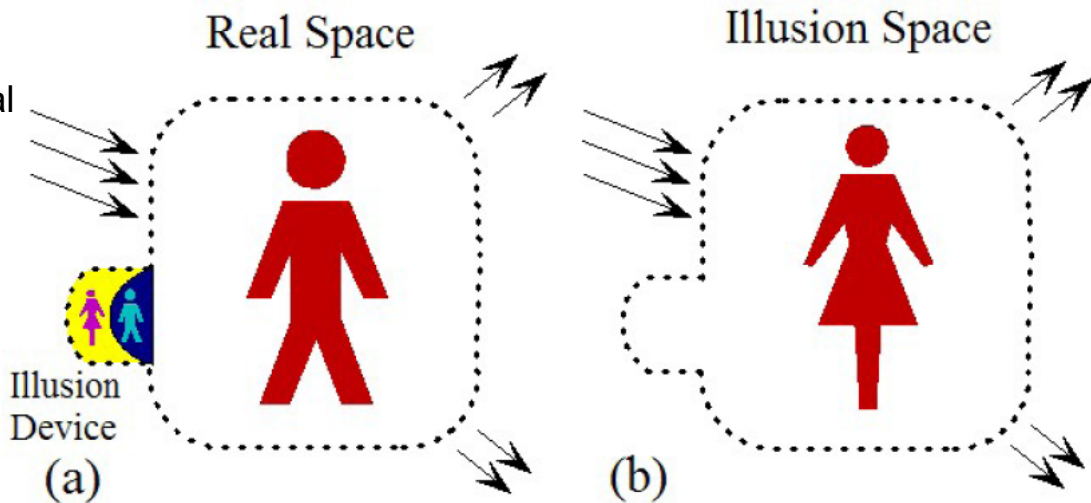
Sep. 18 2015 • Vol 349, Issue 6254

Xingjie Ni,\* Zi Jing Wong,\* Michael Mrejen, Yuan Wang, Xiang Zhang



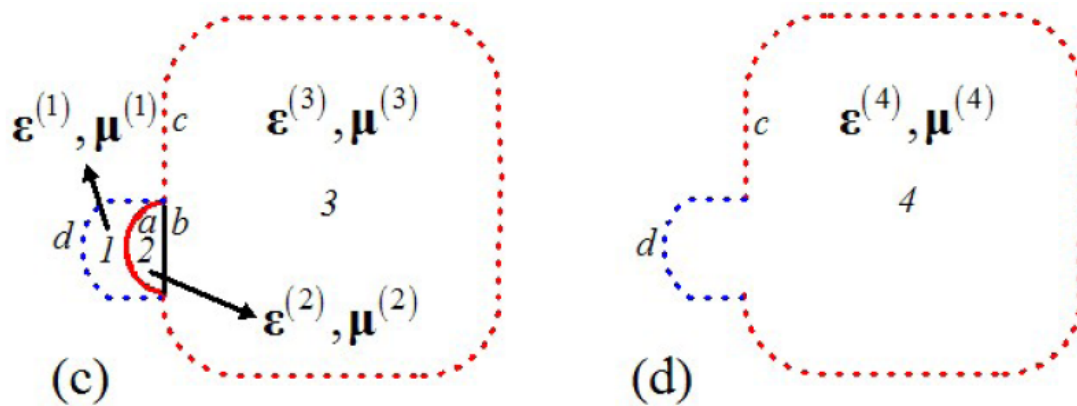
# Optical transformation of one object into another: Optical Illusion

Illusion device can remotely change the optical response



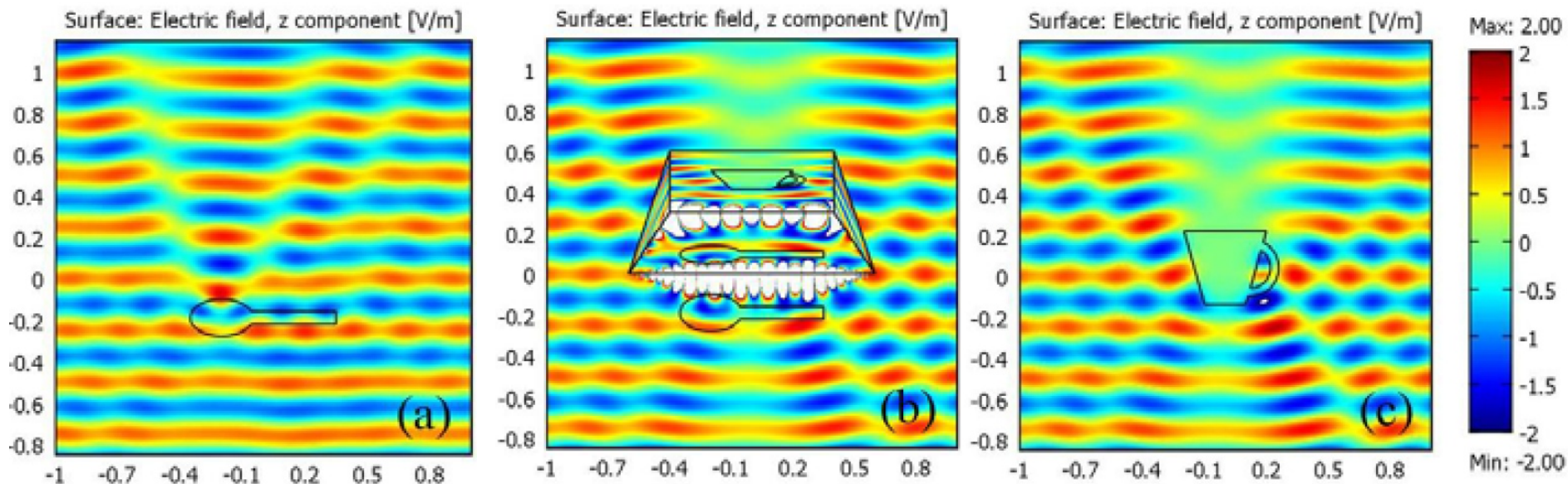
a man (object)

a woman (illusion)



- region 1  
restoring medium
- region 2  
complementary medium
- region 3  
folding region including the man
- region 4  
compressing region including the woman

# Numerical demonstration of the illusion optics



Object:  
dielectric spoon of  $\epsilon_0=2$

scattering pattern

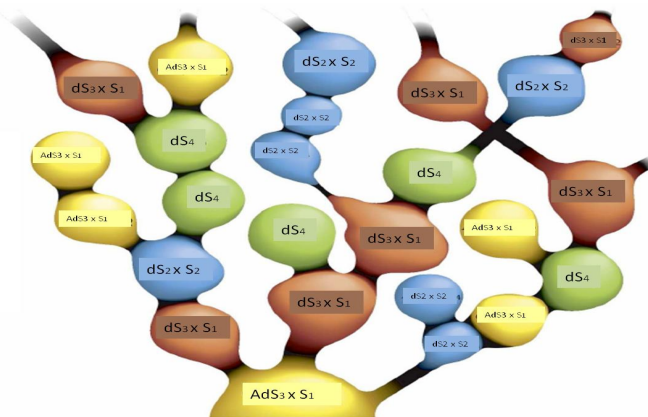
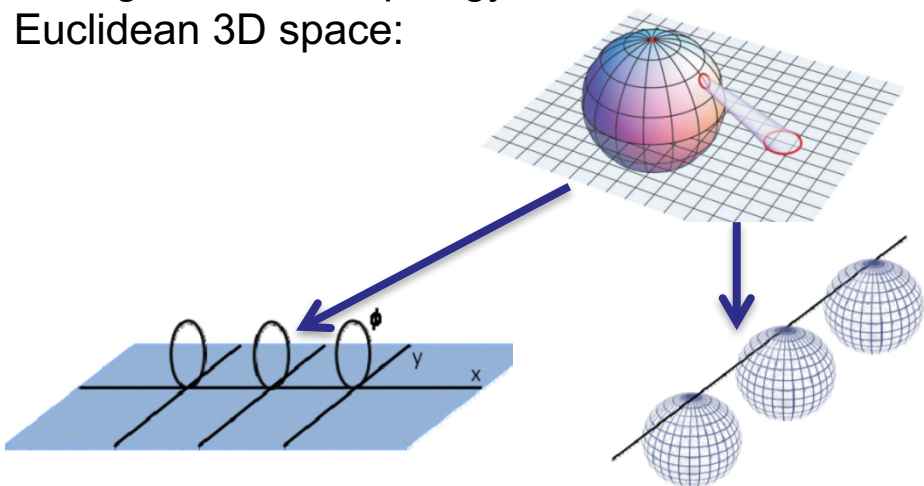
Illusion:  
metallic cup of  $\epsilon_i=-1$

Scattering pattern of a dielectric spoon is changed by the illusion device.  
Outside the virtual boundary, the scattering pattern becomes the same as that of a metallic cup



# Metamaterial "Multiverse" (Smolyaninov)

Using transformation optics we can create "optical spaces" having non-trivial topology, which cannot normally fit into Euclidean 3D space:

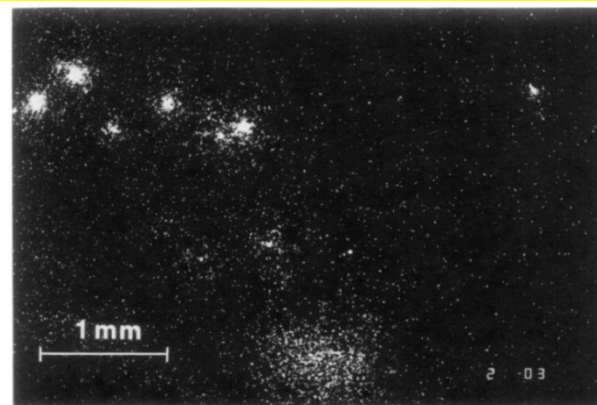


Modern cosmology describes Universe as collection of spaces connected by black holes and wormholes. These spaces may have different topology and different number of dimensions.

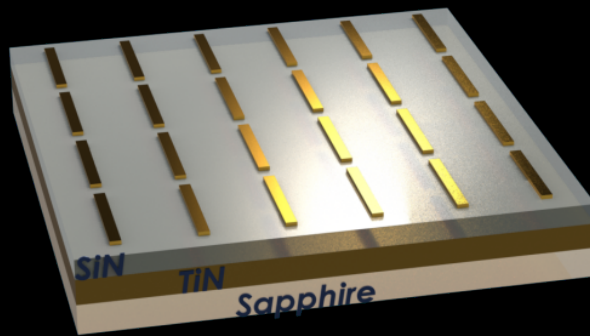
Even metric signature of the "optical space" may differ from the (+ - - -) signature of the Minkowski space. In hyperbolic materials (Smolyaninov, Narimanov – PRL, 2010):

$$\frac{\partial^2 \varphi}{c^2 \partial t^2} = \frac{\partial^2 \varphi}{\epsilon_1 \partial z^2} + \frac{1}{\epsilon_2} \left( \frac{\partial^2 \varphi}{\partial x^2} + \frac{\partial^2 \varphi}{\partial y^2} \right) \quad \begin{matrix} \epsilon_1 < 0 \\ \epsilon_2 > 0 \end{matrix}$$

$$\left( \frac{\partial^2}{\partial x_1^2} + \frac{\partial^2}{\partial x_2^2} - \frac{\partial^2}{\partial x_3^2} - \frac{\partial^2}{\partial x_4^2} \right) \varphi = 0 \quad \text{2T K-G}$$



Flashes of light are observed during metric signature transitions : toy Big Bang physics



# Metasurfaces

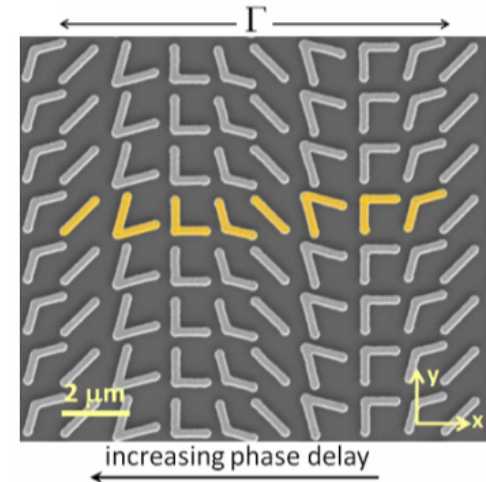
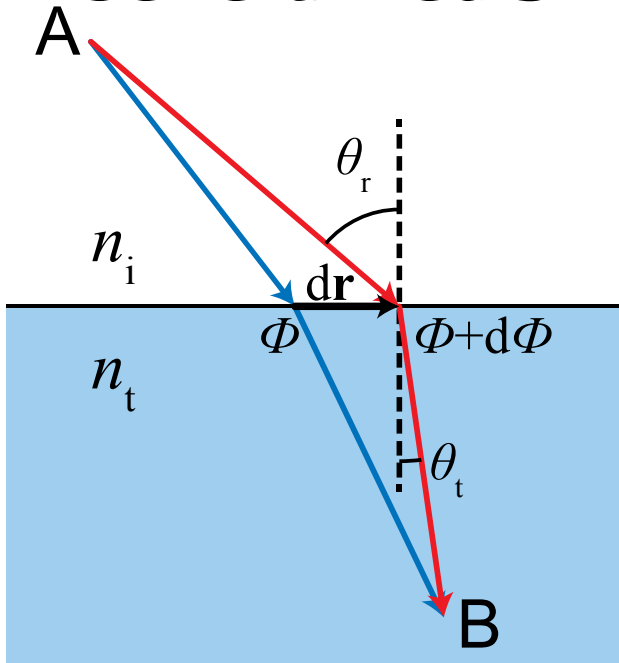
## Review:

A.V. Kildishev, A. Boltasseva, V.M. Shalaev,  
Planar Photonics with Metasurfaces, *Science* **339**, 6125 (2013)

## Early and seminal work on metasurfaces:

E. Hasman, N. Zheludev, F. Capasso, S. Bozhevolnyi. ...

# Generalized Snell's Law (Capasso group)



N. Yu, et al. Science, 2011 (Capasso Group)

Principle of least action → The difference between blue and red path is zero



**For reflection**

$$\sin\theta_r - \sin\theta_i = n_i^{-1} k_0^{-1} \nabla\Phi$$

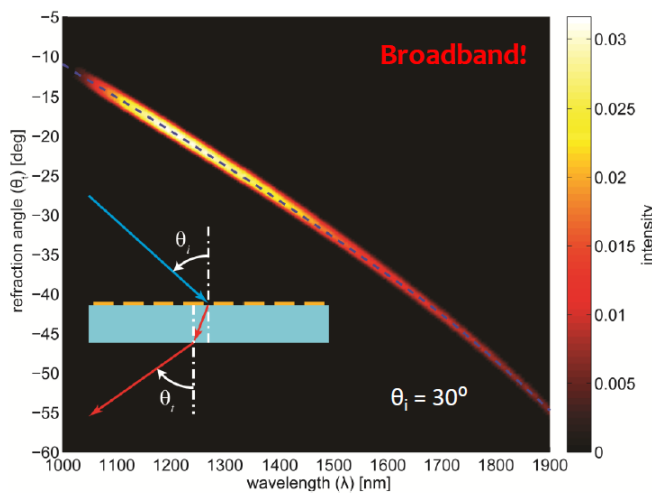
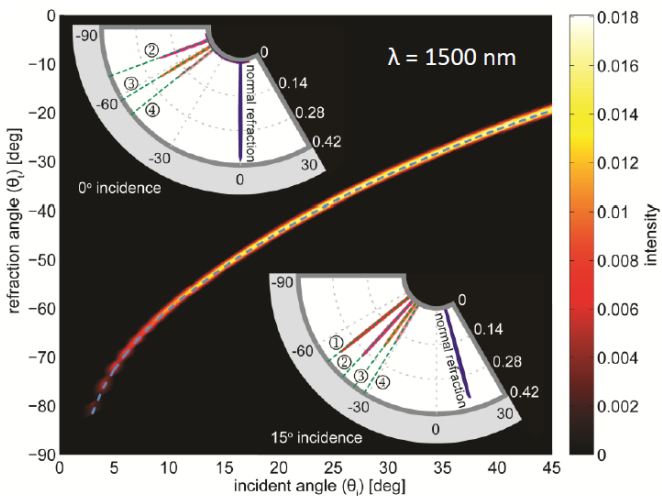
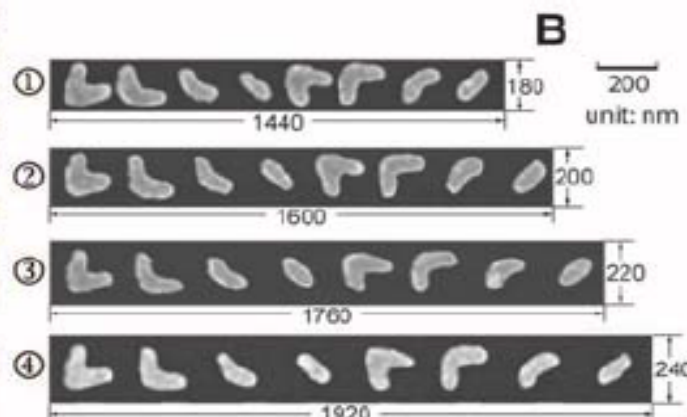
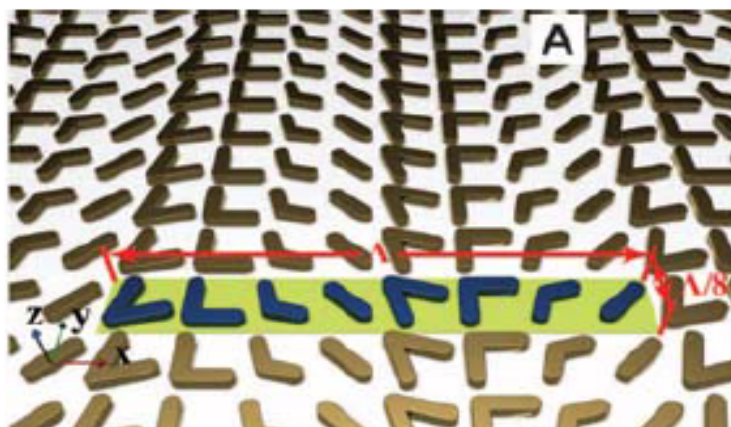
**For refraction**

$$n_t \sin\theta_t - n_i \sin\theta_i = k_0^{-1} \nabla\Phi$$

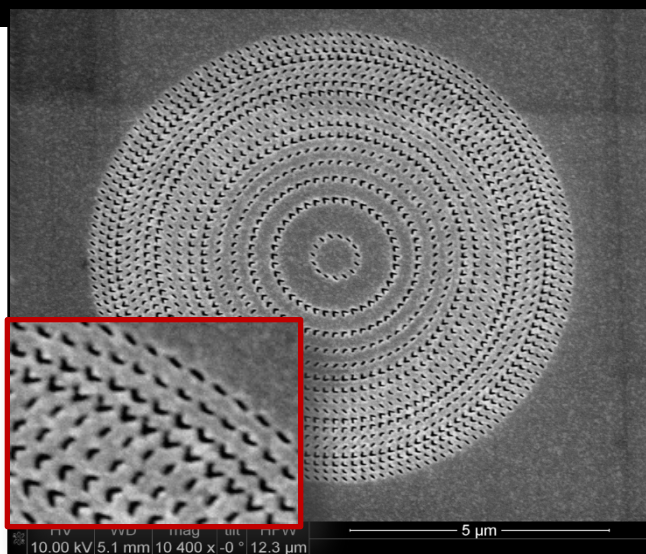
# Broadband Light Bending

Operating at 1–1.9  $\mu\text{m}$

Ni et al, *Science* 335 (2012)  
(Shalaev group)



# Meta-lens and Meta-holograms



Ni et al, *LSA* 2, e72, (2013)

See also:

Meta-lens:

- Aieta et al., *Nano Lett.* 12, 4932 (2012) (Capasso group)
- Chen et al., *Nat Comm* 3, 1198 (2012) (S. Zhang & Zentgraf groups)

Meta-holograms:

- S. Larouche et al., *Nat. Mat.* 11, 450 (2012) (D Smith group)
- Lin et al, *Nano Lett* 13, 4269 (2013) (Capasso group)
- Huang et al, *Nano Lett* 15, 3122 (2015) (Tsai group)
- Zheng et al, *Nat Nanotechnology* 10, 308 (2015) (Guixin Li, Zentgraf, S Zhang groups)
- Kuznetsov et al, *Sci Reports* 5, 7738 (2015)



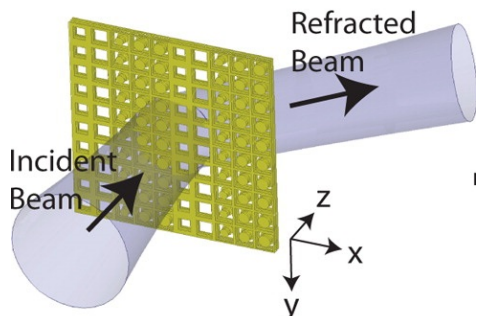
Ni et al, *Nat Comm* 4, 2807 (2013)

Bozhevolnyi group:

Gap plasmons for metasurfaces

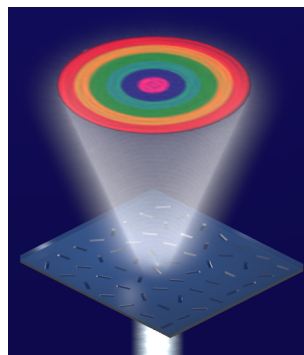
# Metasurface optical devices

## Huygens' surfaces

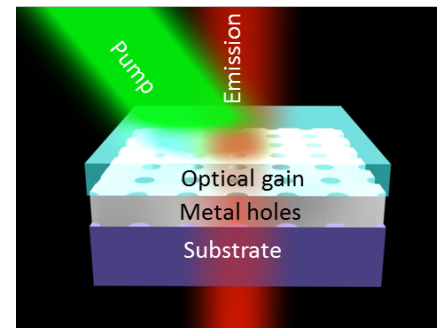


C Pfeiffer et. al., *Nano Lett.*, 14 (5), 2014

## Color Hologram

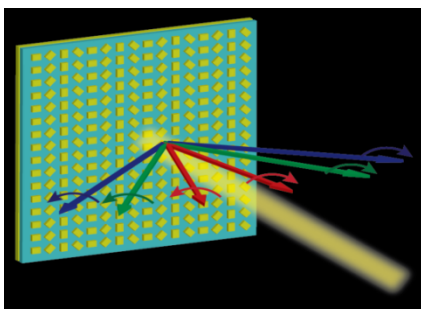


## Active metasurface for lasing



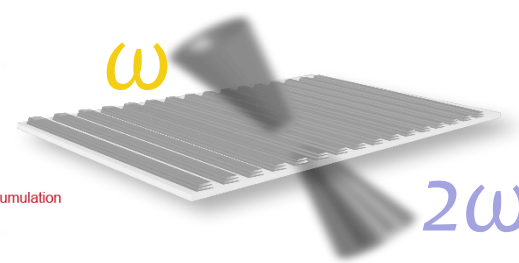
X. Meng et al, *LPR* (2014)

## CD Spectrometer



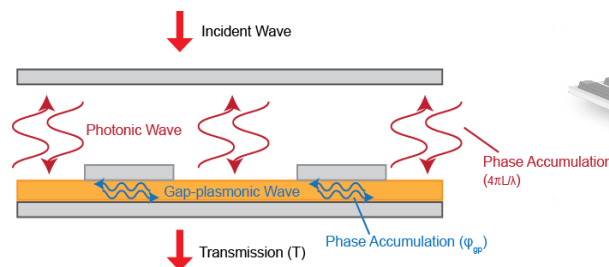
A. Shaltout et. al., *Optica* 2015

## SHG with metasurfaces

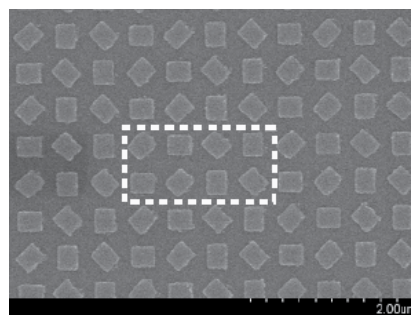


R. Chandrasekar et al, *OMEX* (2015)

## Nanocavity

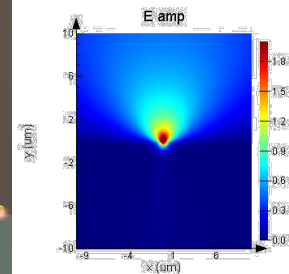
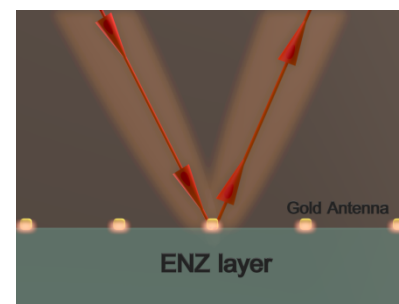


## Broadband Optical Rotator

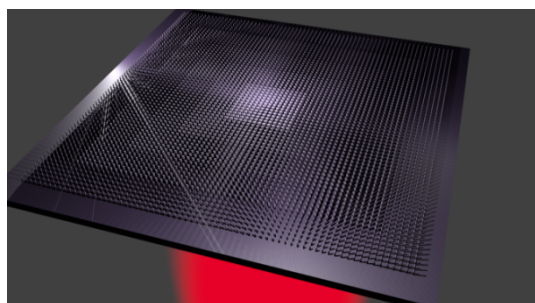


D. Fang et al, *ACS Nano* (2015)

## Antenna on ENZ



## Dielectric Metasurface Lens



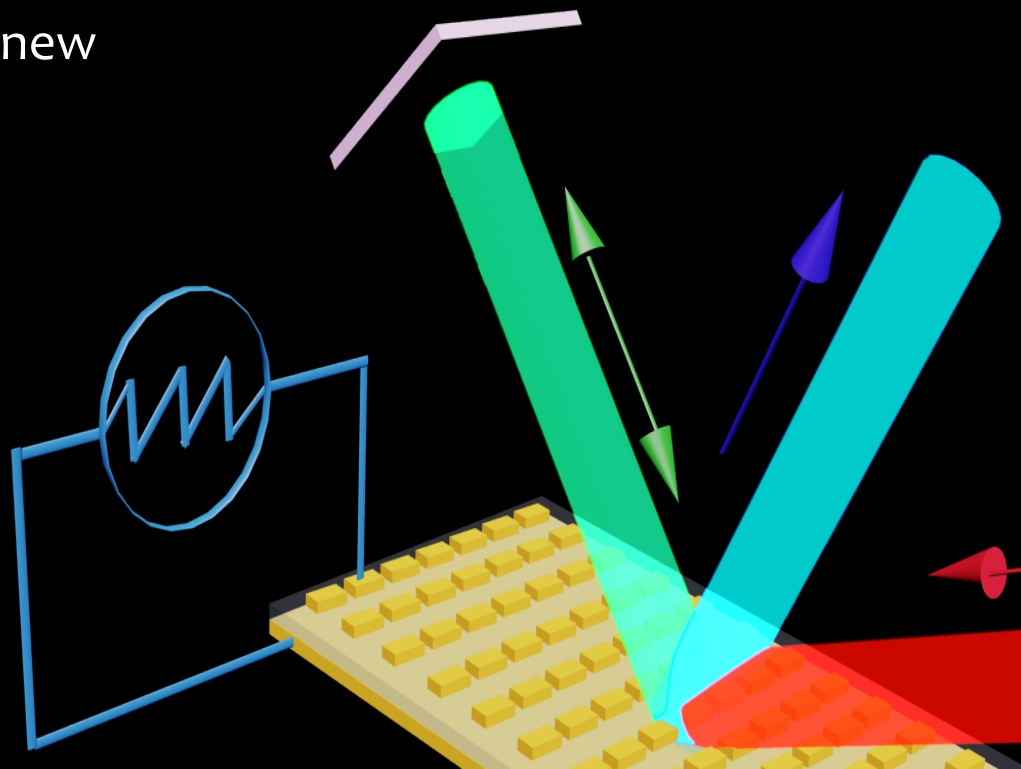
P. R. West, et al, *Opt. Express*, (2014)

# Time-Gradient Metasurfaces

Space-gradient metasurfaces relaxed Snell relation.

Time-gradient Metasurfaces enable new effects:

- Non-reciprocal Snell relation
- Doppler-like wavelength shift
- Energy exchange with light

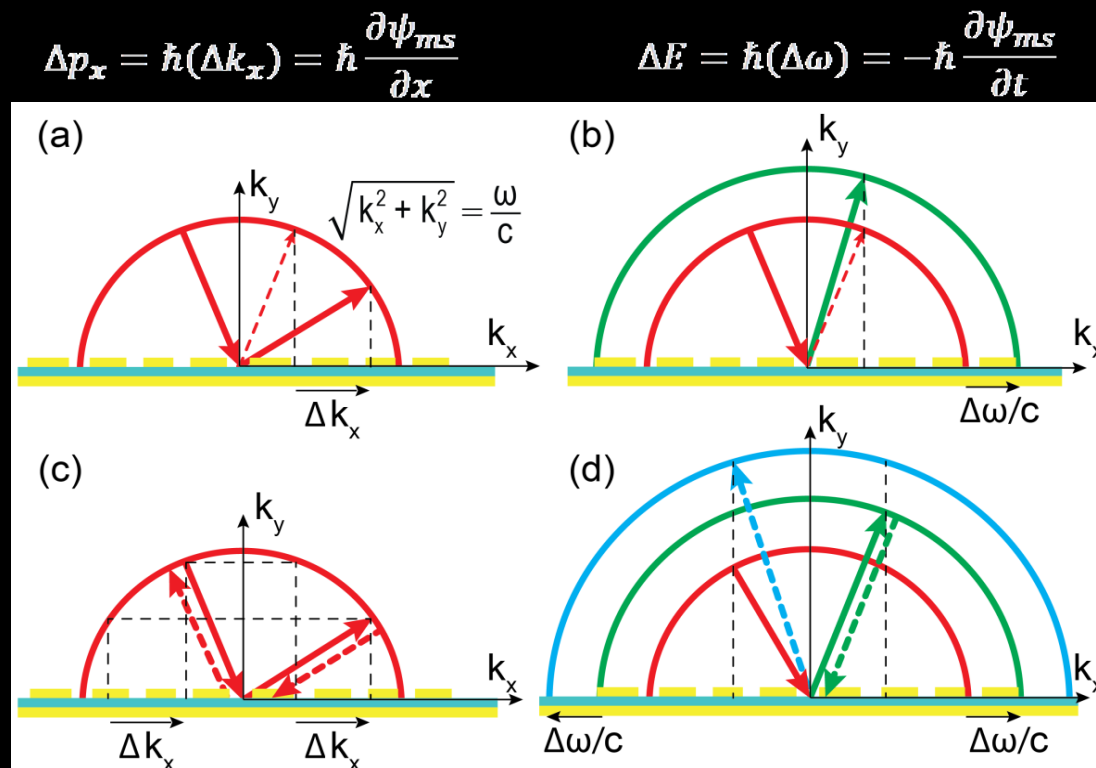


Shaltout et al. "Time-Varying Metasurface and Lorentz Non-reciprocity", arXiv 1507.04836 (2015)

See also non-reciprocal EIT effect: Hadad et al, "Space-time Gradient metasurfaces", PRB 92(10), 2015.

# Gradient metasurfaces: conservation laws & Lorentz non-reciprocity

- Conventional Snell's law conserves photon momentum and energy
- Space-gradient metasurface breaks momentum conservation (generalized Snell)
- Time-gradient metasurface breaks photon energy conservation (non-reciprocal universal Snell)



A. Shaltout et al. "Time-Varying Metasurface and Lorentz Non-reciprocity", arXiv 1507.04836 (2015)

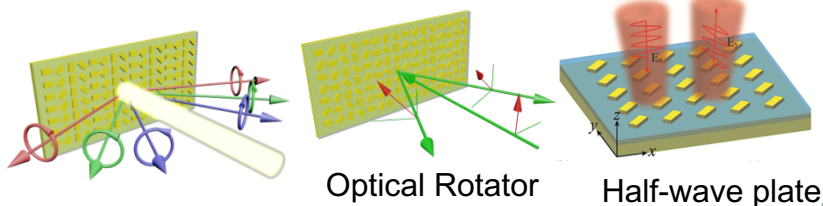
B. See also relevant work by M. Fink on time-reversal applications



# Motivation: Metasurfaces for on-chip Photonics

**Objective:** *unified on-chip metasurface platform* for photonic devices & systems

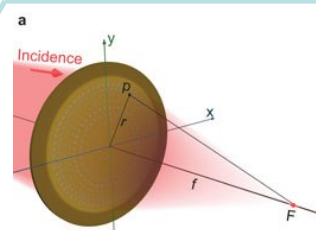
## Polarization Control Devices



Circular Dichroism Spectrometer

Optica, 2(10), 860 (2015)  
ACS Nano, 9(4), 4111 (2015)

## Phase Control devices



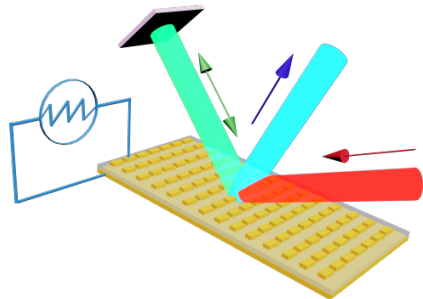
Meta-lens



Meta-hologram

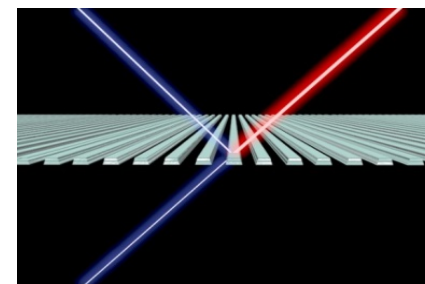
**All-around  
Optical  
Control**

## Non-Reciprocal Devices



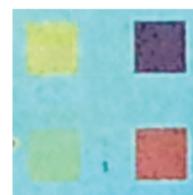
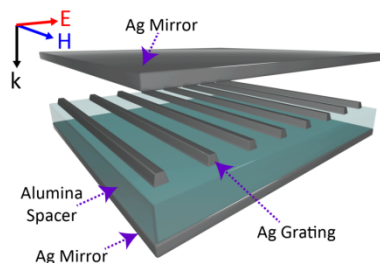
Time-Varying Metasurface  
OMEX, 5(11), 2459 (2015)

## Optical Non-linear Devices



Second Harmonic Generation  
OMEX, 5(11), 2682 (2015)

## Nano-Cavities & Color filters



# What we discussed today

## Metamaterials:

- Electrical metamaterials (plasmonics) for nanophotonics
- Magnetic metamaterials and negative refractive index
- Metamaterials for super-resolution
- Optical cloaking
- Metasurfaces



# METAMATERIALS

“Everything you look at can become a fairy tale and you can get a story from everything you touch.”

— Hans Christian Andersen